

# Three-Particle Final State Energy Distributions: $T+D \rightarrow n+\alpha+\gamma$ and $T+T \rightarrow 2n+\alpha$

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3 December 2013

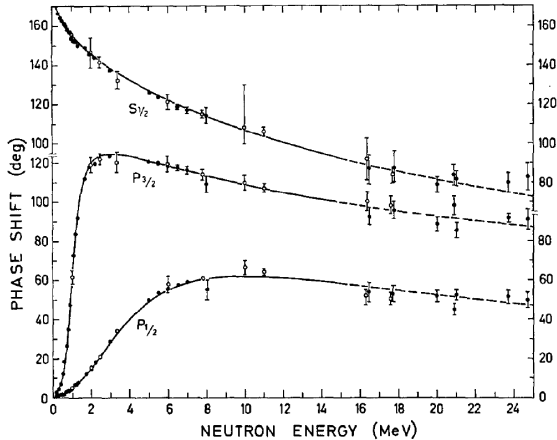
Los Alamos National Laboratory – Seminar



## $T(d, \gamma)^5\text{He}^*$ and $T(t, 2n)\alpha$

- ▶ Both play an important role in inertial confinement fusion:
  - $T(d, \gamma)^5\text{He}^*$ :  $\gamma$  rays  $\rightarrow$  GRH
  - $T(t, 2n)\alpha$ : neutron  $\rightarrow$  NTOF, MRS
- ▶ Both involve the unbound  $^5\text{He}$  nucleus
- ▶  $\alpha + n$  ( $^5\text{He}$ ) resonances effect the energy distributions
- ▶  $R$ -Matrix description of 3-particle final states?
- ▶ Both final-state energy spectra are not “well known” experimentally

# $^5\text{He}$ Level Properties are Well Known from $^4\text{He}(n, n)$ Studies



Stammbach and Walter (1972)

# Determinations of the widths of these states may differ...

Nuclear Physics **A366** (1981) 299-319  
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## REACTION DEPENDENCE OF NUCLEAR DECAY LINEWIDTHS

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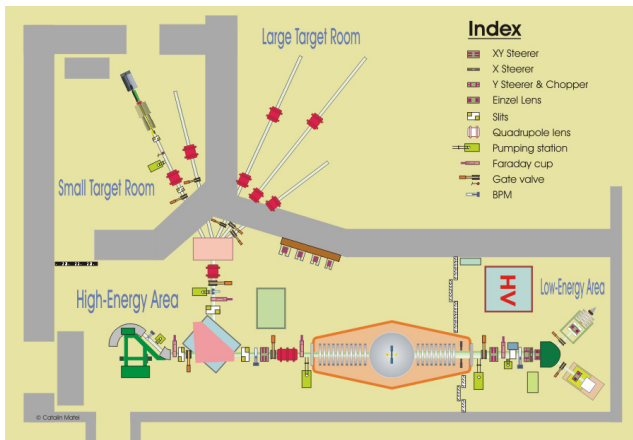
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- ▶ Energy dependence of penetrability factors
- ▶ 3-body final-state interactions
- ▶ Coherent interference with other processes of the same  $J^\pi$
- ▶ Background from processes with possibly different  $J^\pi$
- ▶ → Observed linewidth may vary with reaction and kinematics
- ▶ Well-studied for the first  $2^+$  state in  $^8\text{Be}$

# Edwards Accelerator Laboratory



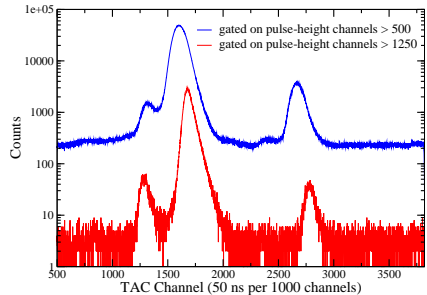
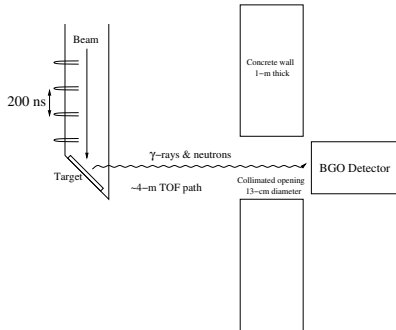
- ▶ 4.5-MV Tandem Accelerator
- ▶ Pelletron Upgrade in 2011/12 via \$321k NSF MRI grant
- ▶ Unique beam swinger and 30-m TOF tunnel
- ▶ Specializations: TOF techniques, neutrons
- ▶ <http://inpp.ohiou.edu/~oual/>



Association for Research  
at University Nuclear Accelerators

# ${}^3\text{H}(d, \gamma)$ Branching Ratio and Photon Spectrum

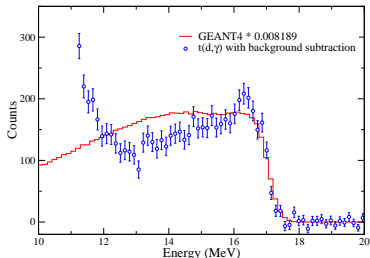
Used as a  $\gamma$ -ray diagnostic for the National Ignition Facility. Both the branching ratio relative to  ${}^3\text{H}(d, n)$  and the  $\gamma$ -ray spectrum are important.



A pulsed 500-keV deuteron beam was used in conjunction with a stopping-thickness solid  ${}^3\text{H}$  target at the Edwards Accelerator Laboratory. A 4"  $\times$  4" BGO detector placed in the beam swinger tunnel  $\approx$  4 m from the target. Key personnel: Cody Parker, Tom Massey, Carl Brune.

Time-of-flight spectra for two pulse-height gates.

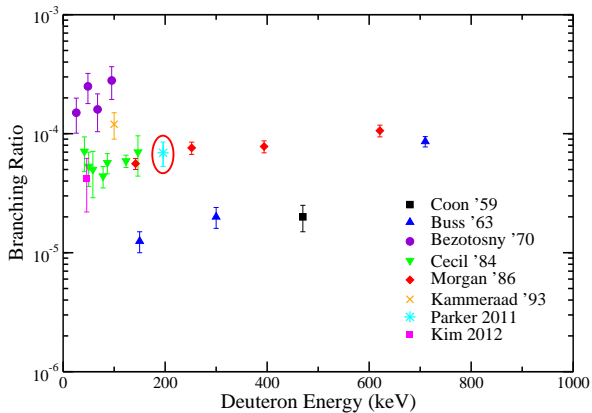
# ${}^3\text{H}(d, \gamma)$ Results and Future Plans



Background-subtracted  $\gamma$ -ray spectrum and Monte Carlo prediction for shape.

- ▶  $\langle E_{c.m.} \rangle = 196$  keV
- ▶  $R = (6.9 \pm 1.6) \times 10^{-5}$
- ▶ Several improvements are underway:
  - new low-mass target holder
  - fresh tritium target
  - $\alpha$ -particle monitor
- ▶ Talk to Cody Parker for more details
- ▶ Theoretical work planned at TRIUMF (P. Navratil)

# Comparison to Previous Work





## $R$ -Matrix Model for ${}^3\text{H}(d, \gamma)$

- ▶ In general, the full suite of partial waves in the initial and final state and  $\gamma$ -ray multipolarities would need to be considered:

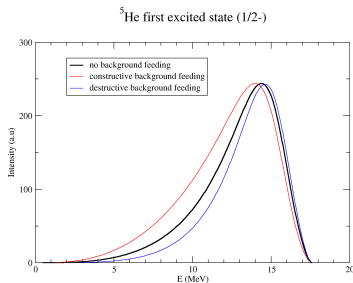
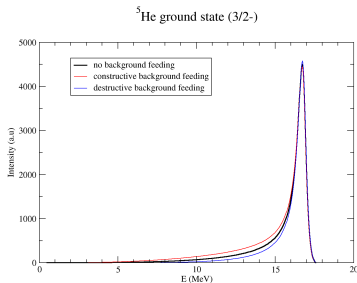
$$\frac{d\sigma}{dE_\gamma} \propto |\langle d + t | H_{EM} | n + \alpha \rangle|^2$$

- ▶ Limiting ourselves to  $3/2^+$  in the initial state and considering  $E1$  transitions to the  $1/2^-$  and  $3/2^-$  final states is reasonable
- ▶ Use  $R$ -matrix formulas (following Barker):

$$\frac{d\sigma}{dE_\gamma} = E_\gamma^3 P_l \left| \frac{\sum_\lambda \frac{A_\lambda \gamma_\lambda}{E_\lambda - E}}{1 - (S_l - B + iP_l)R} \right|^2 \quad R = \sum_\lambda \frac{\gamma_\lambda^2}{E_\lambda - E}$$

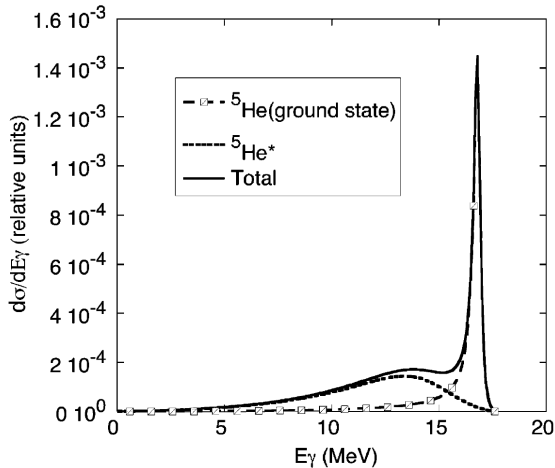
- ▶ Includes penetrabilities and coherent interference
- ▶  $E_\lambda$  and  $\gamma_\lambda$  are determined from  $n - \alpha$  elastic scattering
- ▶  $A_\lambda$  are  $\gamma$ -ray feeding factors
- ▶ Only 2 levels are needed for both final states

# $R$ -Matrix Results for ${}^3\text{H}(d, \gamma)$



- ▶ Colored curves show possible effects of coherent interference ( maximum plausible)
- ▶ Similar to “Hale Spectrum”
- ▶ Except the present  $3/2^-$  width is 0.70 MeV – versus 0.50 MeV and there is more strength in the tail of the  $3/2^-$  peak

# Hale Spectrum: “Two-Body Resonance Model”



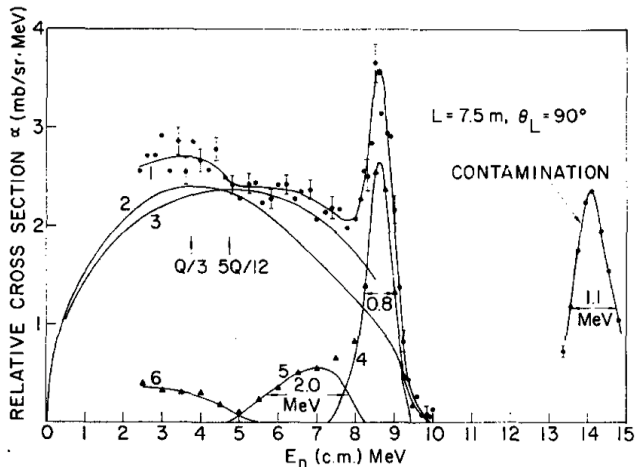
J.M. Mack, G.M. Hale et al., Rad. Phys. and Chem. **75** 551-556 (2006).

$$T(t, 2n)\alpha$$

- ▶ Wong, Anderson et al. results (1965)
- ▶  $R$ -matrix model
- ▶ National Ignition Facility results
- ▶ Role of di-neutron emission?
- ▶ How to resolve ambiguities?
- ▶  $\alpha$  spectrum?
- ▶  $T(t, 2n)$  absolute cross section?
- ▶  ${}^3\text{He}({}^3\text{He}, 2p)\alpha$  and  ${}^3\text{He}(t, np)\alpha$

# $T(t, 2n)\alpha$ Neutron Spectrum

$$E_{c.m.} = 200 \text{ keV}$$



Wong, Anderson, and McClure (1965)

# $T(t, 2n)\alpha$ $R$ -Matrix Modeling

Carl Brune, Dan Sayre, Jac Caggiano, Gerry Hale, Mark Paris

- ▶ Sequential decay model
- ▶ Kinematics (recoil) is more complicated
- ▶ Angular correlation effects on spectrum
- ▶ Identical particles / antisymmetrization
- ▶ F.C. Barker formalism + angular momentum coupling + antisymmetrization
  - D.P. Balamuth, R.W. Zurmühle, and S.L. Tabor, Phys. Rev. C **10**, 975 (1974).
  - D.F. Geesaman *et al.*, Phys. Rev. C **15**, 1835 (1977).
  - H.O.U. Fynbo *et al.*, Phys. Rev. Lett **91**, 082502 (2003).

# Some Formulas

- Our form for the matrix element:

$$\mathcal{M}_{\nu_1\nu_2} = \sum_c u_c(12) f_{\nu_1\nu_2}^{lJ}(\Omega_1, \Omega_{23}) - u_c(21) f_{\nu_2\nu_1}^{lJ}(\Omega_2, \Omega_{13})$$

- $u_c$  is given by an  $R$ -matrix expression:

$$u_c(12) = \left[ \frac{P_1 P_{23}}{p_1 p_{23}} \right]^{1/2} e^{i(\omega_1 - \Phi_1)} e^{i(\omega_{23} - \Phi_{23})} \frac{\sum_{\lambda} \frac{A_{c\lambda} \gamma_{c\lambda}}{E_{c\lambda} - E_{23}}}{1 - [S_{23} - B_c + iP_{23}] R_c}$$

- $f_{\nu_1\nu_2}^{lJ}$  contains the spin and angular information:

$$f_{\nu_1\nu_2}^{lJ}(\Omega_1, \Omega_{23}) = \sum_{m, m_l, m_l'} \frac{(-1)^{J+m}}{\sqrt{2J+1}} \langle l m_l \frac{1}{2} \nu_1 | J m \rangle \langle l m_l' \frac{1}{2} \nu_2 | J - m \rangle Y_{l m_l}(\hat{\mathbf{p}}_1) Y_{l m_l'}(\hat{\mathbf{p}}_{23})$$

- The particle distribution is given by

$$\frac{d^3 N}{dE_i \Omega_i d\Omega_j} = \sum_{\nu_1, \nu_2} |\mathcal{M}_{\nu_1\nu_2}|^2 p_i p_{jk} \mathcal{J}_{ijk}$$

- A  $0^+$  ( $l=0$ ) initial  $t+t$  state is assumed, and  $c = 1/2^+, 1/2^-, 3/2^-$   $n + \alpha$  or an  $l=0$  spin-singlet dineutron state.

# The resulting formula for the particle spectra...

is not so simple, and I will not repeat it here. The key step is the application of an obscure addition theorem for spherical harmonics that was first given by M.E. Rose [Journal of Mathematics and Physics **37**, 215 (1958)]:

$$Y_{lm}(\hat{\mathbf{c}}) = \sum_{\substack{\lambda_1 + \lambda_2 = l \\ \nu_1 + \nu_2 = m}} a^{\lambda_1} b^{\lambda_2} \langle \lambda_1 \nu_1 \lambda_2 \nu_2 | lm \rangle \sqrt{\frac{4\pi(2l+1)!}{(2\lambda_1+1)!(2\lambda_2+1)!}} Y_{\lambda_1 \nu_1}(\hat{\mathbf{a}}) Y_{\lambda_2 \nu_2}(\hat{\mathbf{b}}),$$

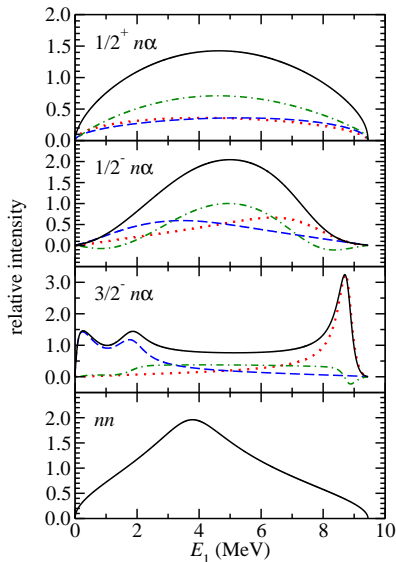
where  $\hat{\mathbf{c}} = \vec{\mathbf{a}} + \vec{\mathbf{b}}$  with  $\vec{\mathbf{a}} = a\hat{\mathbf{a}}$  and  $\vec{\mathbf{b}} = b\hat{\mathbf{b}}$ .



## Findings:

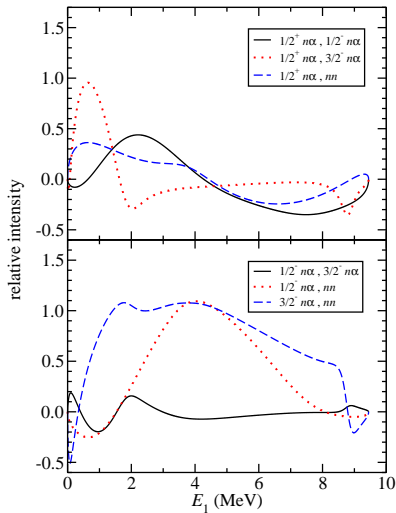
- ▶ Antisymmetrization is very important
- ▶ Angular correlations are important for the  $3/2^- \ n + \alpha$  channel
- ▶ There *is* coherent interference between different partial waves

# Neutron Energy Distributions



Neutron energy distributions for each channel considered separately. The primary, secondary, exchange, and total are given by the dotted, dashed, dot-dashed, and solid curves, respectively. Only the total is shown for the  $nn$  case.

# Coherent Interference Effects

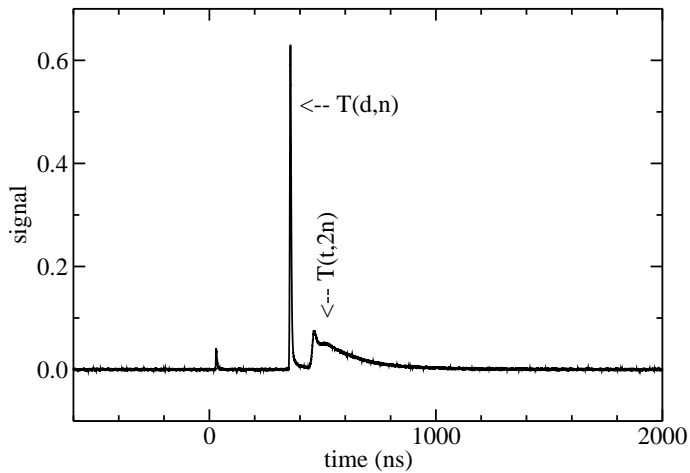


- Interference contributions to the neutron energy distributions for partial wave combinations indicated.
- There is minimal coherent interference between the  $3/2^-$  and  $1/2^-$  contributions.

# Measurement of the $T(t, 2n)\alpha$ Neutron Spectrum at the National Ignition Facility

- ▶ Nearly pure tritium gas (0.1% D), low areal density “symcap”
- ▶  $kT = 3.3(3)$  keV  $\rightarrow E_{\text{Gamow}}(\text{T} + \text{T}) = 16$  keV
- ▶ 2 organic liquid scintillators (xylene) @ 20 and 22 meters, respectively
- ▶ Modeling includes:
  - ▶ Instrument Response Function (time response)
  - ▶ Scintillator response (efficiency)
  - ▶ Attenuation and scattering
  - ▶ Thermal broadening
  - ▶ Background from  $T(d, n)$  (small)
- ▶ Dan Sayre, Jac Caggiano, Robert Hatarik, Chris Hagmann, Tom Phillips, and many additional collaborators (including CRB and ADB).

# Raw Data from Equator Detector @ 20.1 m

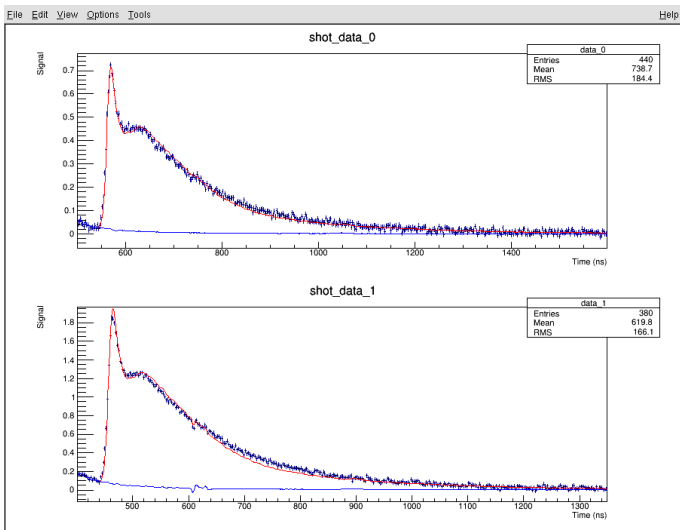


## $R$ -Matrix Fit

- ▶ Assume  $3/2^-$  and  $1/2^-$   $n$ - $\alpha$  channels.
- ▶ Use the Stambach and Walter  $n$ - $\alpha$   $R$ -matrix parameters
- ▶ Fit both detectors simultaneously
- ▶ Achieve  $\chi^2_\nu = 2.2$  (statistical errors are complicated)
- ▶ Results:

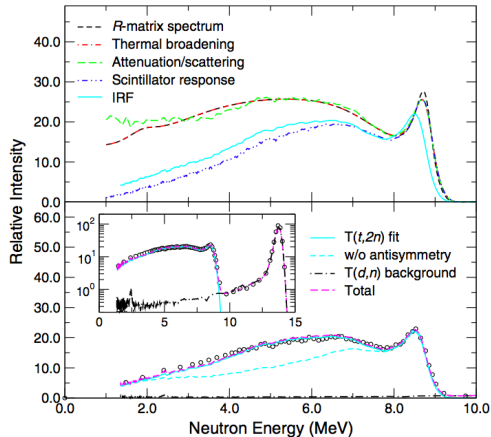
$J^\pi$	$\lambda$	$E_\lambda$ (MeV)	$\gamma_\lambda^2$ (MeV)	$A_\lambda$
$3/2^-$	1	0.97	7.55	11.1
$3/2^-$	2	100.0	30.0	157
$1/2^-$	1	6.43	12.3	19.6
$1/2^-$	2	100.0	30.0	689

# Fits to Time Spectra



# $T(t, 2n)\alpha$ Neutron Spectrum

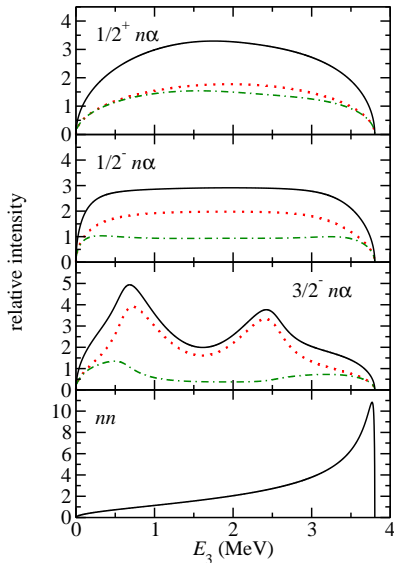
$E_{c.m.} = 16$  keV



Sayre, Caggiano et al. (2013) @ NIF



# $\alpha$ Particle Energy Distributions



Alpha-particle energy distributions for each channel considered separately. The primary plus secondary, exchange, and total are given by the dotted, dot-dashed, and solid curves, respectively. Only the total is shown for the  $nn$  case.

# $T(t, 2n)\alpha$ Neutron Spectrum Summary / Open Questions

- ▶ Only the  $3/2^-$  ( $^5\text{He}$  g.s.) provides a distinct feature
- ▶ Interpretation of the continuum remains ambiguous
  - could this be addressed by a correlation measurement?
- ▶  $\alpha$  spectrum?
- ▶  $T(t, 2n)$  absolute cross section?

# Jarmie and Brown, NIM B10/11 405 (1985)

## Measured $\alpha$ s – preliminary results...

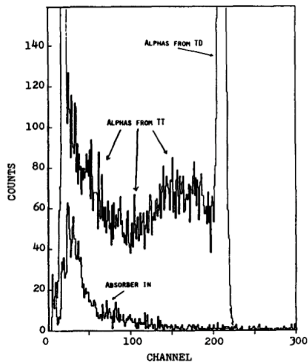


Fig. 8.  $T(t, \alpha)nn$  reaction raw data for  $45^\circ$  lab angle and 115 keV bombarding energy. Note the large peak of alpha-particles from the 0.5% deuterium contaminant in the target gas.

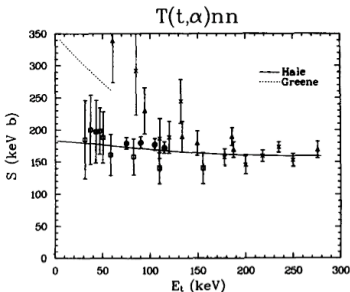
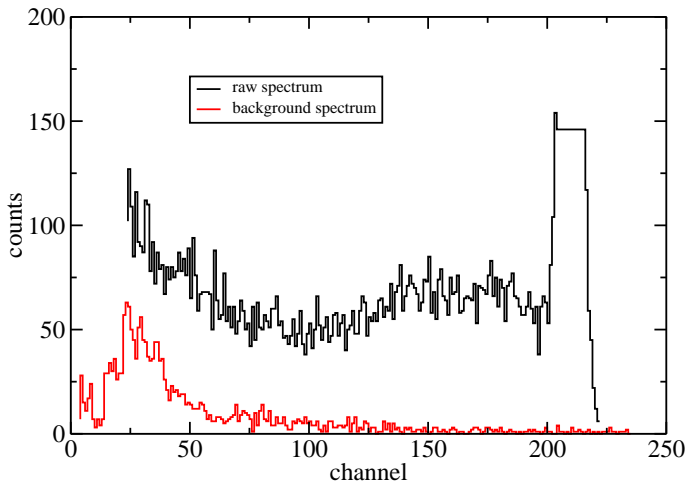
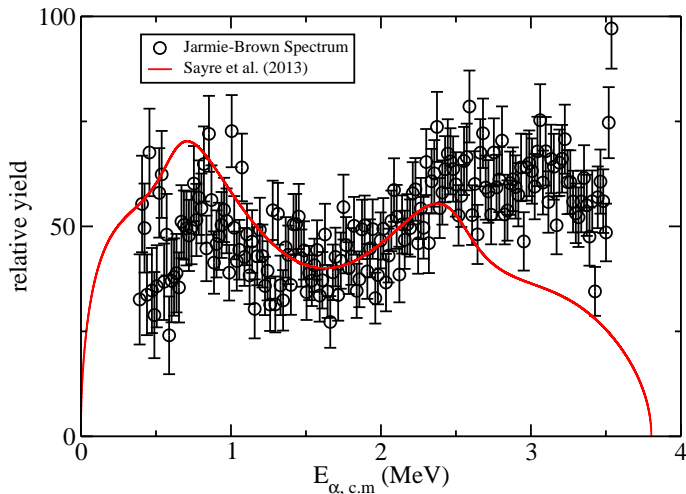


Fig. 9. Integrated  $S$  functions for the  $T(t, \alpha)nn$  reaction. Our preliminary data are the black circles with 5% absolute errors. Also shown are the data of Gonorov et al. (triangles) ref. [10]; Agnew et al. (crosses) [11]; and Serov et al. (squares) [12]. The solid curve is an  $R$ -matrix prediction of Hale [13], and the dashed curve is from the compilation of Greene [14].

# Jarmie-Brown Spectrum

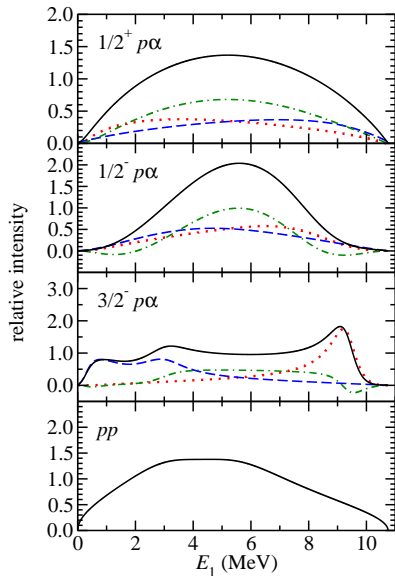


# Jarmie-Brown Spectrum Compared to Sayre *et al.* (2013) R-Matrix Fit



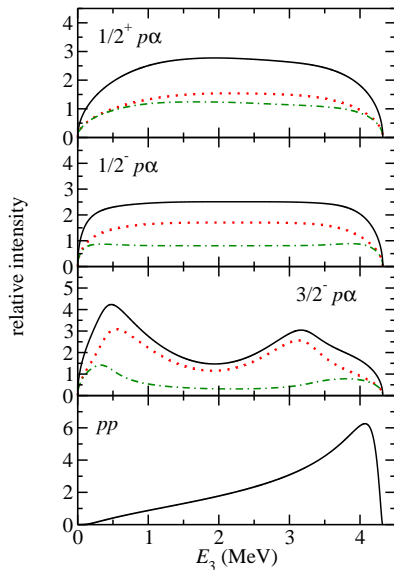
Suggestive of di-neutron strength?

# Proton Energy Distributions from ${}^3\text{He} + {}^3\text{He}$



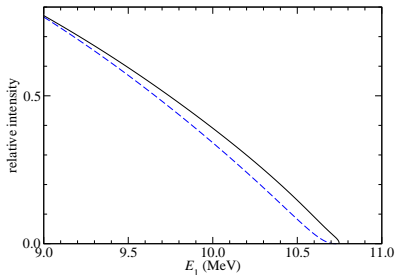
Proton energy distributions from  ${}^3\text{He} + {}^3\text{He}$  for each channel considered separately. The primary, secondary, exchange, and total are given by the dotted, dashed, dot-dashed, and solid curves, respectively. Only the total is shown for the  $pp$  case.

# $\alpha$ Energy Distributions from ${}^3\text{He} + {}^3\text{He}$



Alpha-particle energy distributions from  ${}^3\text{He} + {}^3\text{He}$  for each channel considered separately. The primary, secondary, exchange, and total are given by the dotted, dashed, dot-dashed, and solid curves, respectively. Only the total is shown for the  $pp$  case.

# Coulomb Effects Near the Endpoint



Proton energy distributions from  ${}^3\text{He} + {}^3\text{He}$  for the  $1/2^+ p\alpha$  channel near the endpoint. The solid curve is the same as shown previously and the dashed curve shows the effect of including an ad-hoc Coulomb correction.



Thank you for your attention.