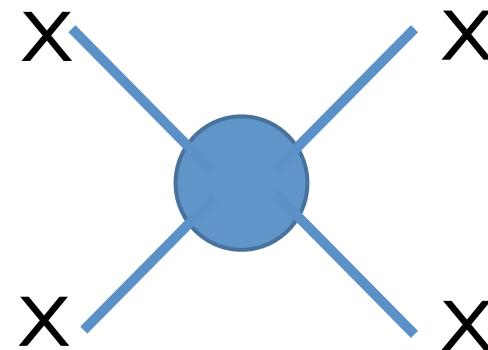


Beyond Collisionless Dark Matter

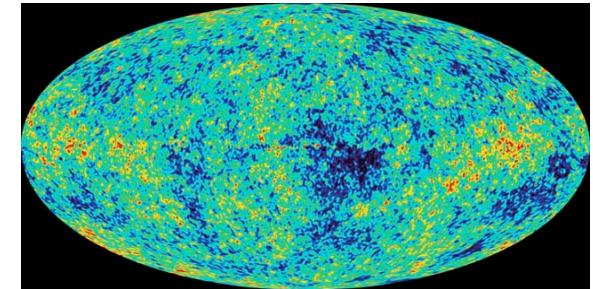
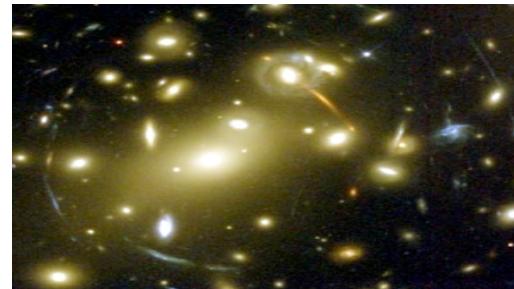
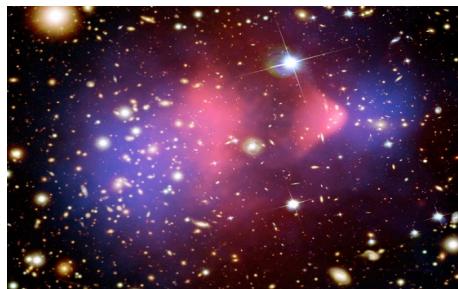
Hai-Bo Yu
University of California, Riverside



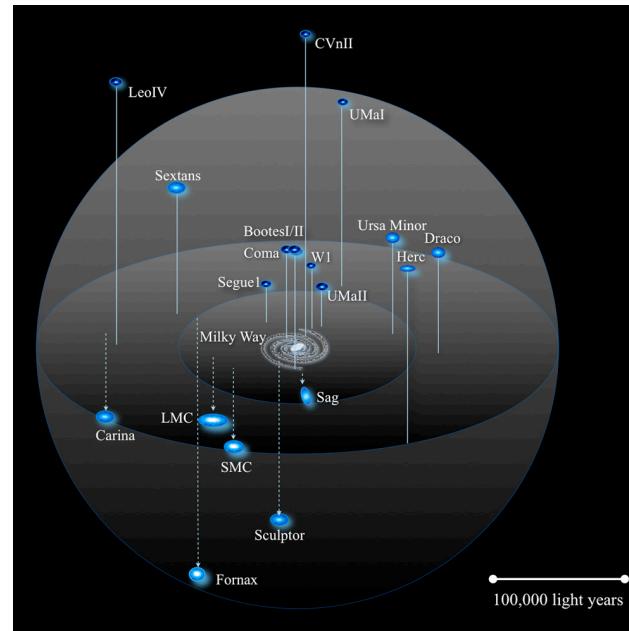
LANL 02/20/2014

Collisionless Cold Dark Matter

- Large scales: very well

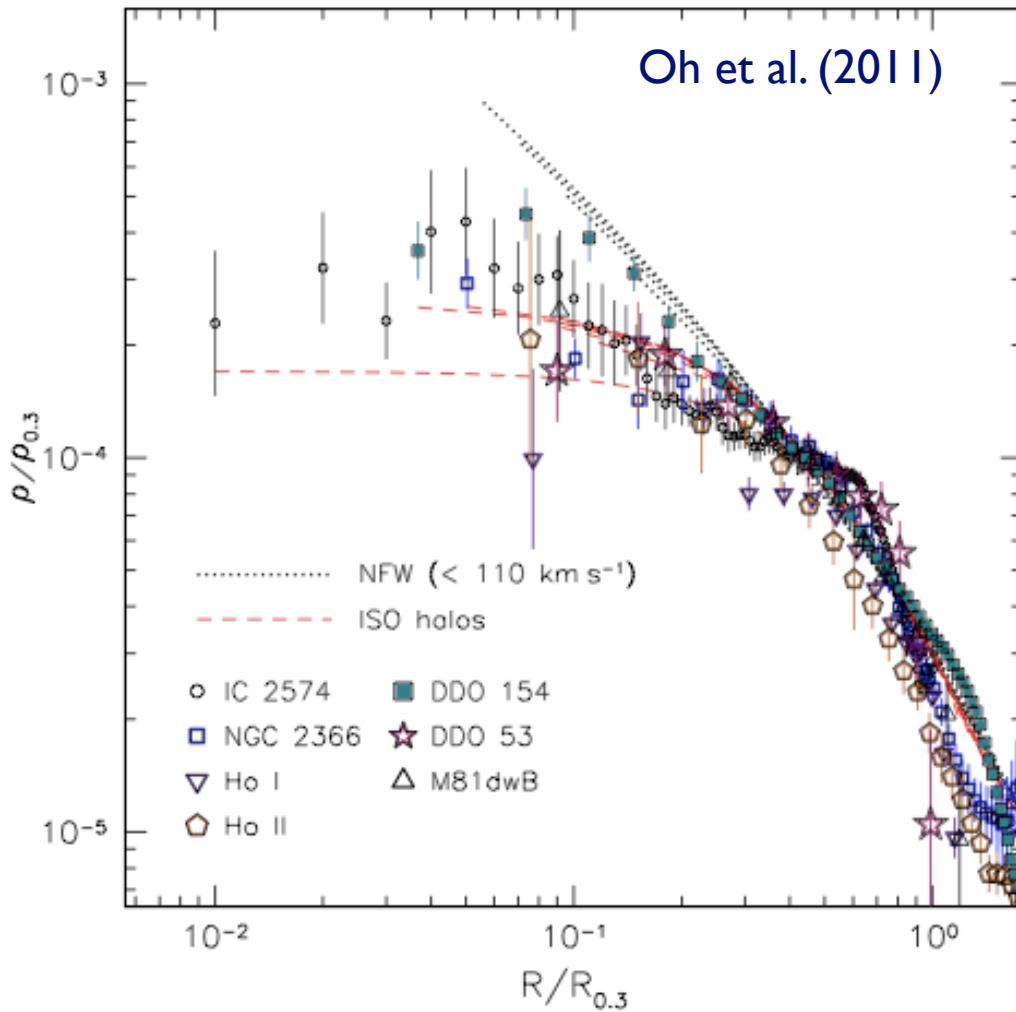


- Small scales (dwarf galaxies, subhalos, even clusters): ?



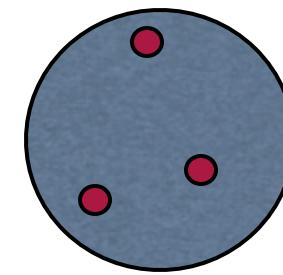
Core VS. Cusp Problem

- THINGS (dwarf galaxy survey)



density profile: $\rho \sim r^\alpha$
predicted: $\alpha \sim -1$
observed: $\alpha = -0.29 \pm 0.07$

- Observed central density shows cores
- CDM-only simulations predict cusps

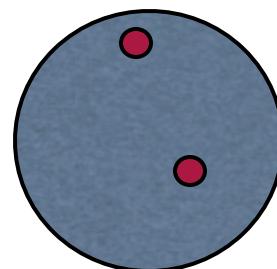
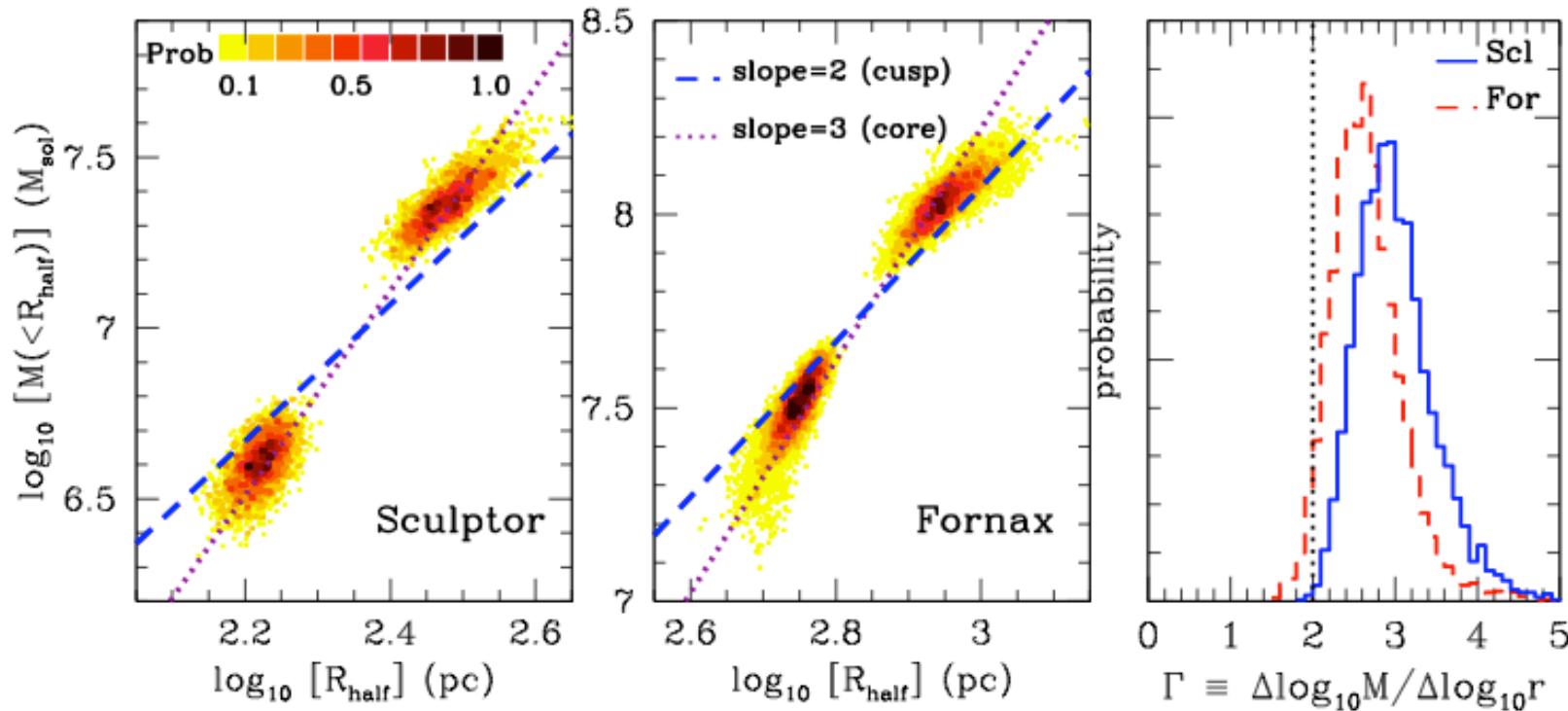


$$V \sim \sqrt{\frac{GM_<}{r}}$$
$$M_< \sim \int \rho r^2 dr$$

Core VS. Cusp Problem

- Milky Way dwarf galaxies

Walker, Penarrubia (2011)



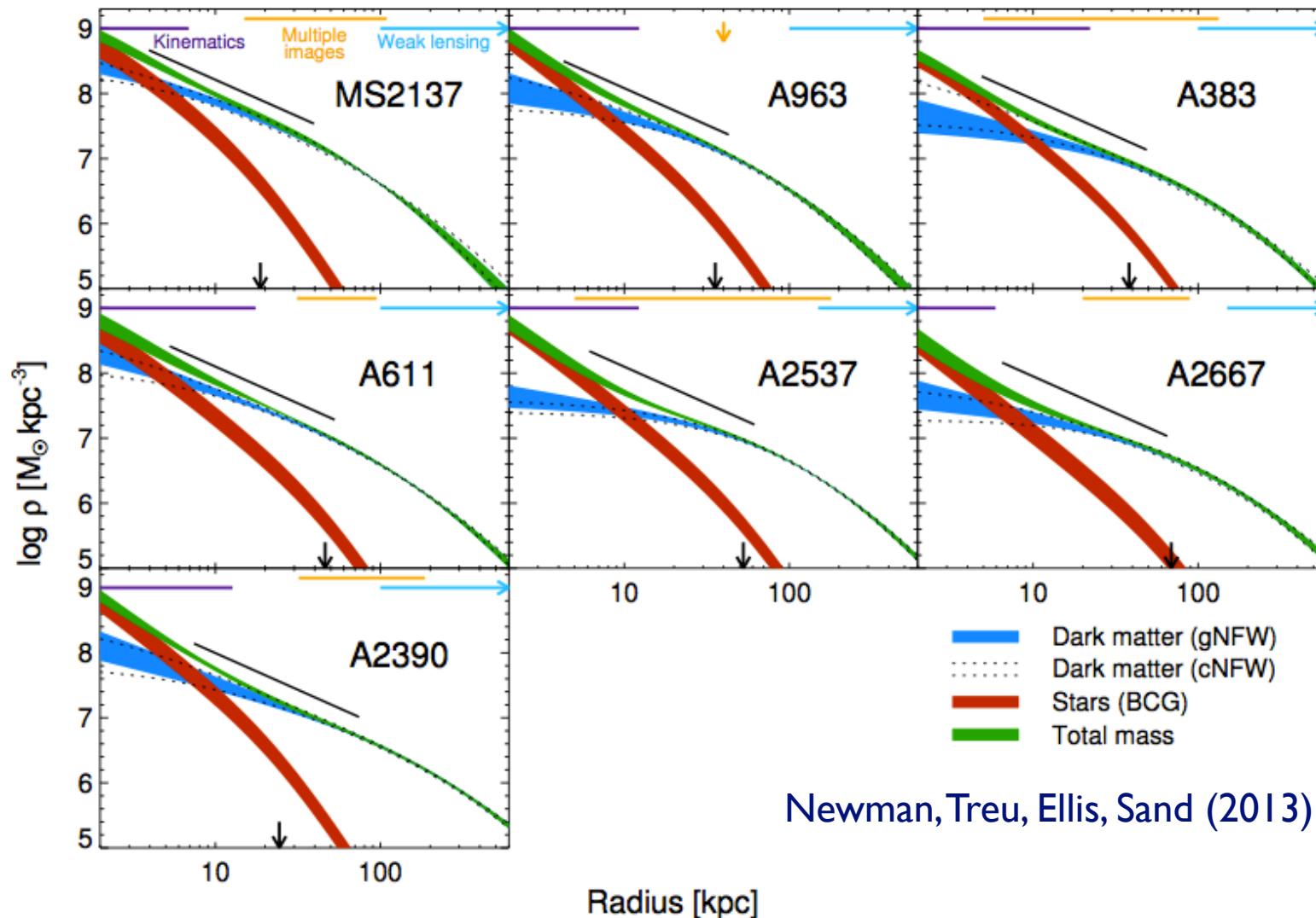
$$V \sim \sqrt{\frac{GM_<}{r}}$$

cusp $\rho \sim r^{-1} \rightarrow M \sim \int \rho d^3r \sim r^2$

core $\rho \sim \text{const} \rightarrow M \sim \int \rho d^3r \sim r^3$

Two groups of stars as test particles

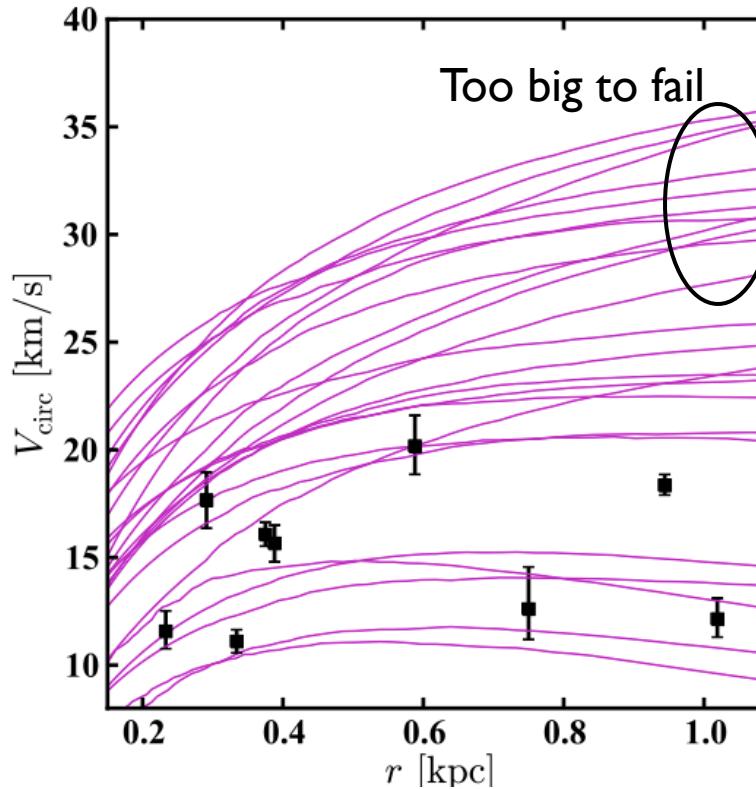
Even Clusters!



Too Big to Fail Problem

- Milky Way dwarf galaxies Boylan-Kolchin, Bullock, Kaplinghat (2011)

$$V \sim \sqrt{\frac{GM_<}{r}}$$



Biggest predicted satellites
from CDM simulations

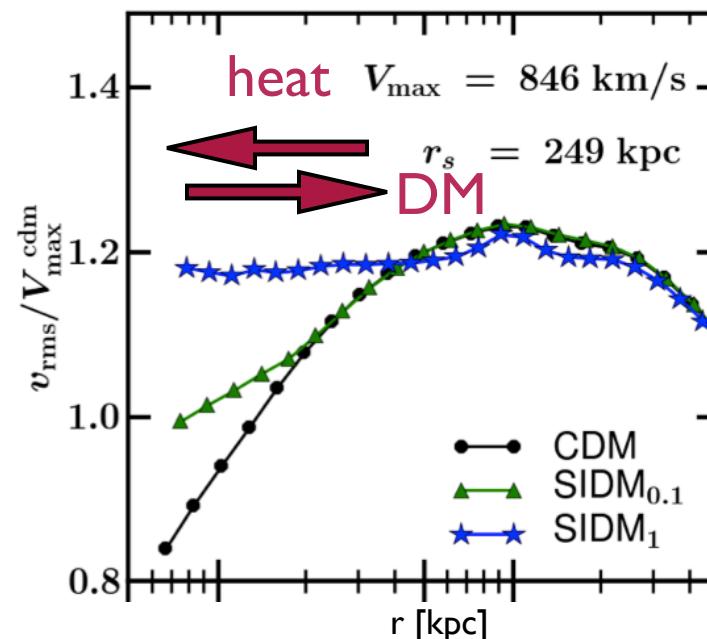
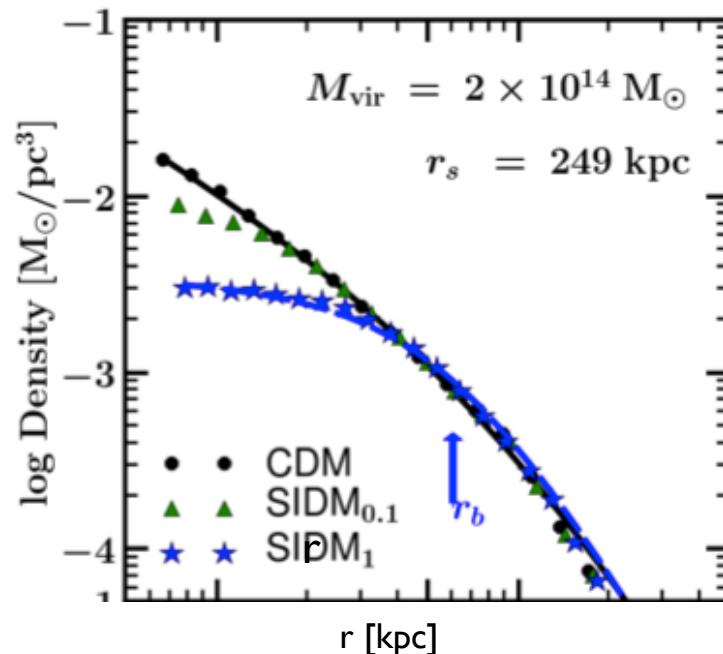
Brightest observed satellites
in the MW

- Most massive subhalos in collisionless CDM simulations are too dense to host observed galaxies in the Milky Way
- On the other hand, it is easier for stars to form in massive subhalos

Self-interacting Dark Matter

- All these anomalies can be solved if DM is strongly self-interacting

Spergel, Steinhardt (1999)



UCI group: Rocha, Peter, Bullock, Kaplinghat, Garrison-Kimmel, Onorbe, Moustakas (2012); Peter, Rocha, Bullock, Kaplinghat (2012)

Harvard group: Vogelsberger, Zavala, Loeb (2012); Zavala, Vogelsberger, Walker (2012)

Self-interactions reduce the central DM density

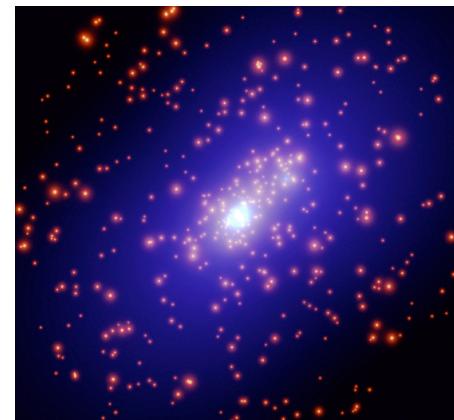
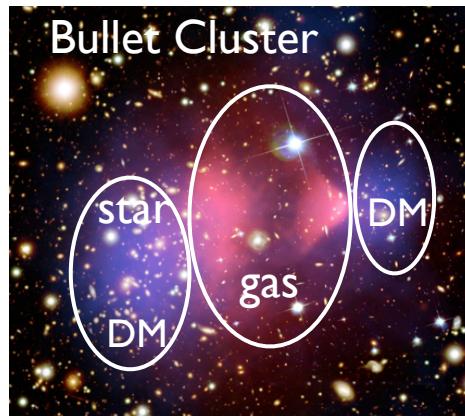
Astrophysics Summary

- Evidence for DM self-interactions on dwarf galaxy scales

$$\sigma/m_X \sim 0.1 - 10 \text{ cm}^2/\text{g} \text{ for } v \sim 10-30 \text{ km/s}$$

$$\Gamma \simeq n\sigma v = (\rho/m_X)\sigma v \sim H_0$$

- **Constraints:** Bullet Cluster; elliptical halo shapes (?)



$\sigma/m_X < 1 \text{ cm}^2/\text{g}$ for 3000 km/s (cluster); $v \sim 300 \text{ km/s}$ (NGC720)

Peter, Rocha, Bullock, Kaplinghat (2012)

NOT $\sigma/m_X < 0.02 \text{ cm}^2/\text{g}$ Miralda-Escude (2000)

Challenges

- A really large scattering cross section! a nuclear-scale cross section

$$\sigma \sim 1 \text{ cm}^2 (m_X/g) \sim 2 \times 10^{-24} \text{ cm}^2 (m_X/\text{GeV})$$

For a WIMP: $\sigma \sim 10^{-38} \text{ cm}^2 (m_X/100 \text{ GeV})$

SIDM indicates a new mass scale

- How to avoid the constraints on large scales?

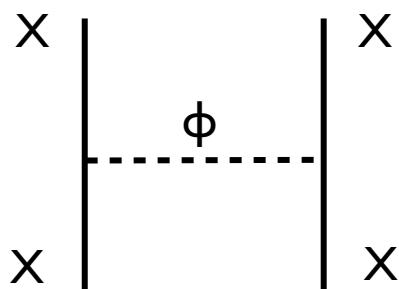
$$\sigma/m_X < 1 \text{ cm}^2/\text{g} \text{ for } 3000 \text{ km/s (cluster)}$$

In particular, if $\sigma \sim \text{constant}$

Spergel, Steinhardt (1999)

Note: the constant cross section is still allowed if $\sigma/m_X \sim 0.5-1 \text{ cm}^2/\text{g}$

Particle Physics of SIDM

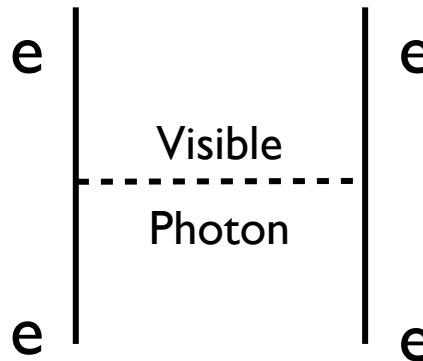


- SIDM indicates light mediators

$$\sigma \approx 5 \times 10^{-23} \text{ cm}^2 \left(\frac{\alpha_X}{0.01} \right)^2 \left(\frac{m_X}{10 \text{ GeV}} \right)^2 \left(\frac{10 \text{ MeV}}{m_\phi} \right)^4$$

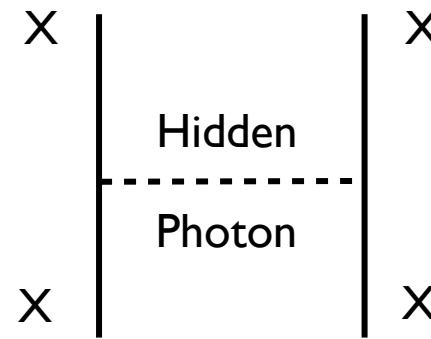
in the perturbative and small velocity limit

- With a light mediator, DM self-scattering is velocity-dependent (like Rutherford scattering)



$$\sigma \sim \frac{\alpha_X^2}{m_X^2 v^4}$$

$m_X v \gg m_\phi$

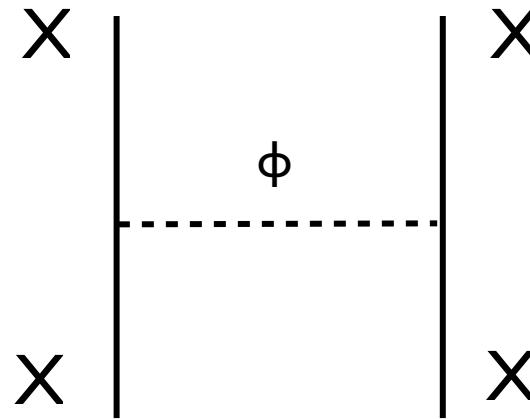


- DM is self-scattering on small scales ($v \sim 10\text{-}30 \text{ km/s}$)
- DM is collisionless on large scales ($v \sim 3000 \text{ km/s}$), specially for heavy SIDM

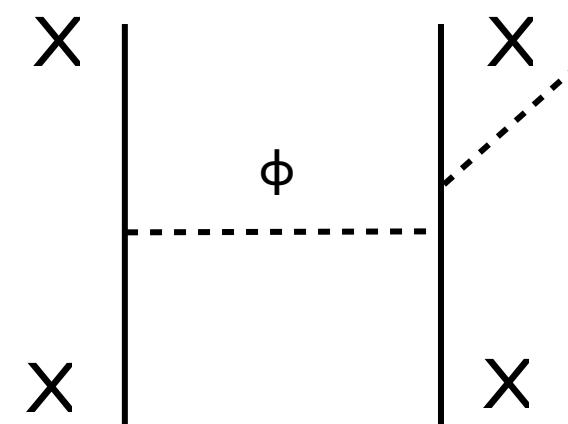
Feng, Kaplinghat, Tu, HBY (2009); Loeb, Weiner (2010)

Not Dissipative

- SIDM is not dissipative

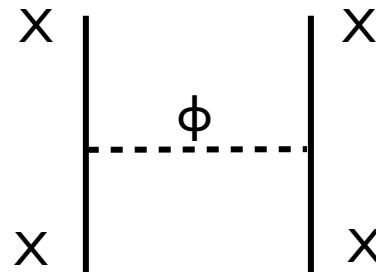


$$\Gamma = n \sigma v \sim H_0$$



$$\Gamma = \alpha_x n \sigma v \ll H_0 \text{ as long as } \alpha_x < 1$$

A Simplified Model



$$\mathcal{L}_{\text{int}} = \begin{cases} g_X \bar{X} \gamma^\mu X \phi_\mu & \text{vector mediator} \\ g_X \bar{X} X \phi & \text{scalar mediator} \end{cases}$$

A Yukawa potential

$$\sigma_T = \int d\Omega (1 - \cos \theta) \frac{d\sigma}{d\Omega}$$

$$V(r) = \pm \frac{\alpha_X}{r} e^{-m_\phi r}$$

$\alpha_X = g_X^2 / (4\pi)$
regulate forward scattering

Map out the parameter space (m_X, m_ϕ, α_X)

- Solve small scale anomalies (small v)
- Avoid constraints on large scales (large v)
- Get the relic density right

Scattering with a Yukawa Potential

$$V(r) = \pm \frac{\alpha_X}{r} e^{-m_\phi r}$$

DM self-scattering

Exception: $m_\phi=0$

Perturbative (Born)
regime

$$\alpha_X m_X / m_\phi \ll 1$$

Feng, Kaplinghat, HBY (2009)

Lin, HBY, Zurek (2011)

Nonperturbative
regime

$$\alpha_X m_X / m_\phi \gtrsim 1$$

Classical
regime

$$m_X v / m_\phi \gg 1$$

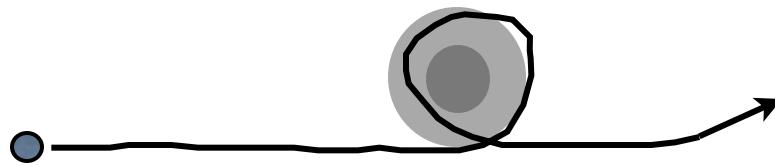
Resonant
regime

$$m_X v / m_\phi \lesssim 1$$

Classical Regime

- Classical approximation from plasma physics

Khrapak et al. (2003) (2004)



Charged-particle
scattering in plasma

$$\pm \frac{\alpha_X}{r} e^{-m_\phi r}$$
$$\alpha_X = \alpha_{\text{EM}}$$

m_ϕ = Debye photon mass

$\sigma_T \sim v^{-4}$ at large v

$\sigma_T \sim \text{const}$ at small v
(saturated)

$$\sigma_T^{\text{clas}} \approx \begin{cases} \frac{4\pi}{m_\phi^2} \beta^2 \ln(1 + \beta^{-1}) & \beta \lesssim 10^{-1} \\ \frac{8\pi}{m_\phi^2} \beta^2 / (1 + 1.5\beta^{1.65}) & 10^{-1} \lesssim \beta \lesssim 10^3 \\ \frac{\pi}{m_\phi^2} \left(\ln \beta + 1 - \frac{1}{2} \ln^{-1} \beta \right)^2 & \beta \gtrsim 10^3 \end{cases}$$

$$\beta \equiv 2\alpha_X m_\phi / (m_X v^2)$$

Apply to DM: σ_T is enhanced on dwarf scales compared to larger scales

Feng, Kaplinghat, HBY (2009); Loeb, Weiner (2010); Vogelsberger, Loeb, Zavala (2012)...

Beyond Perturbation

$$V(r) = \pm \frac{\alpha_X}{r} e^{-m_\phi r}$$

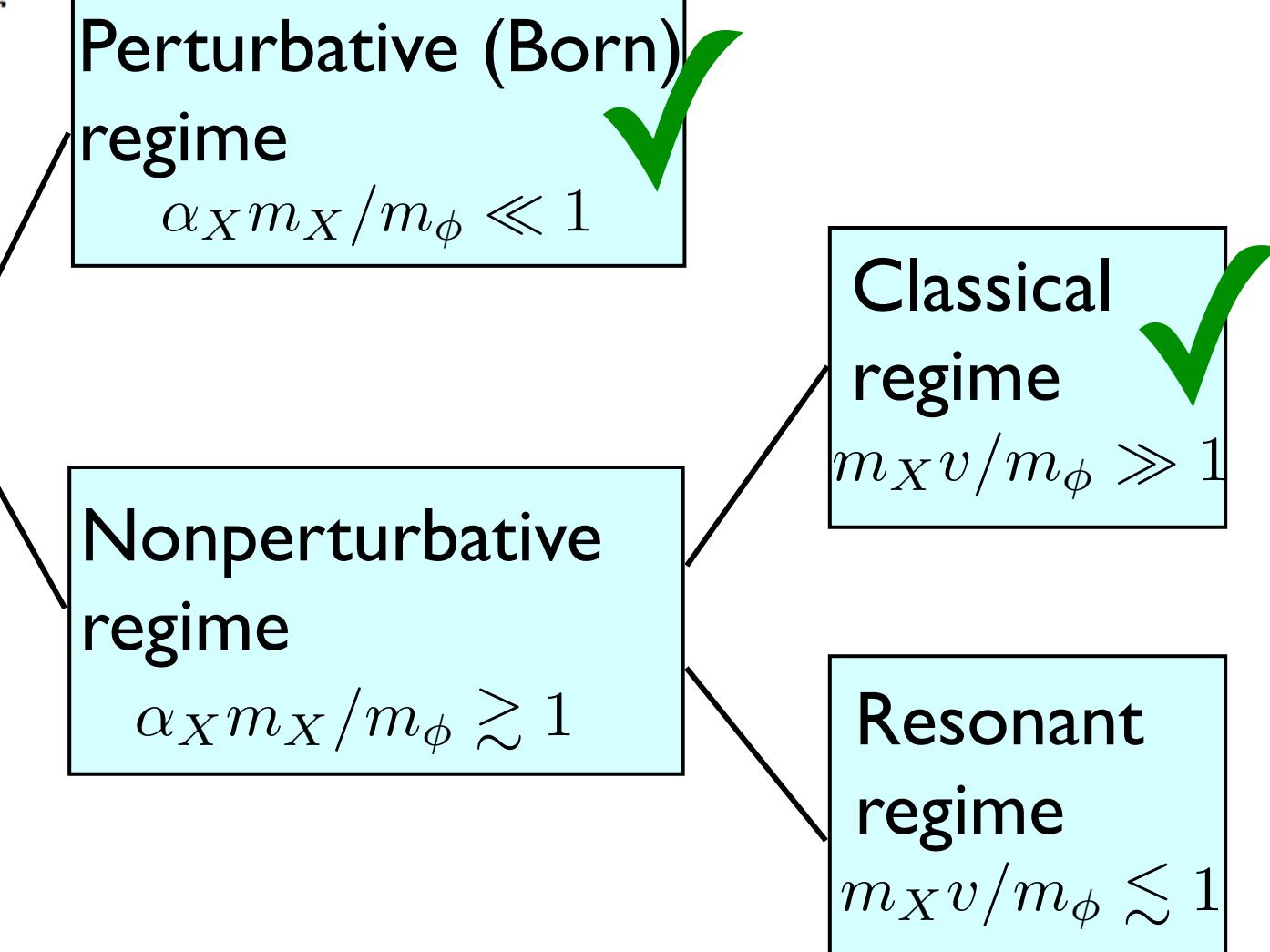
DM self-scattering

Perturbative (Born)
regime
 $\alpha_X m_X / m_\phi \ll 1$

Nonperturbative
regime
 $\alpha_X m_X / m_\phi \gtrsim 1$

Classical
regime
 $m_X v / m_\phi \gg 1$

Resonant
regime
 $m_X v / m_\phi \lesssim 1$



Numerical Approach

- Quantum mechanics 101-partial wave analysis

$$\frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{dR_\ell}{dr} \right) + \left(k^2 - \frac{\ell(\ell+1)}{r^2} - 2\mu V(r) \right) R_\ell = 0$$

- Transfer cross section

$$\frac{d\sigma}{d\Omega} = \frac{1}{k^2} \left| \sum_{\ell=0}^{\infty} (2\ell+1) e^{i\delta_\ell} P_\ell(\cos \theta) \sin \delta_\ell \right|^2 \quad \sigma_T = \int d\Omega (1 - \cos \theta) \frac{d\sigma}{d\Omega}$$

$$\frac{\sigma_T k^2}{4\pi} = \sum_{\ell=0}^{\infty} [(2\ell+1) \sin^2 \delta_\ell - 2(\ell+1) \sin \delta_\ell \sin \delta_{\ell+1} \cos(\delta_{\ell+1} - \delta_\ell)]$$

Rearrange $\ell \rightarrow \ell + 1$

$$\frac{\sigma_T k^2}{4\pi} = \sum_{\ell=0}^{\infty} (\ell+1) \sin^2(\delta_{\ell+1} - \delta_\ell)$$



Tulin, HBY, Zurek (2012)(2013)

Both formulas are identical in the limit of $\ell \rightarrow \infty$
But the second one converges much faster

Numerical Approach

- Partial wave analysis

$$\frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{dR_\ell}{dr} \right) + \left(k^2 - \frac{\ell(\ell+1)}{r^2} - 2\mu V(r) \right) R_\ell = 0$$

- Boundary conditions $r \rightarrow \infty$

$$R_\ell(r) \rightarrow \sin(kr - \pi\ell/2 + \delta_\ell)/r$$

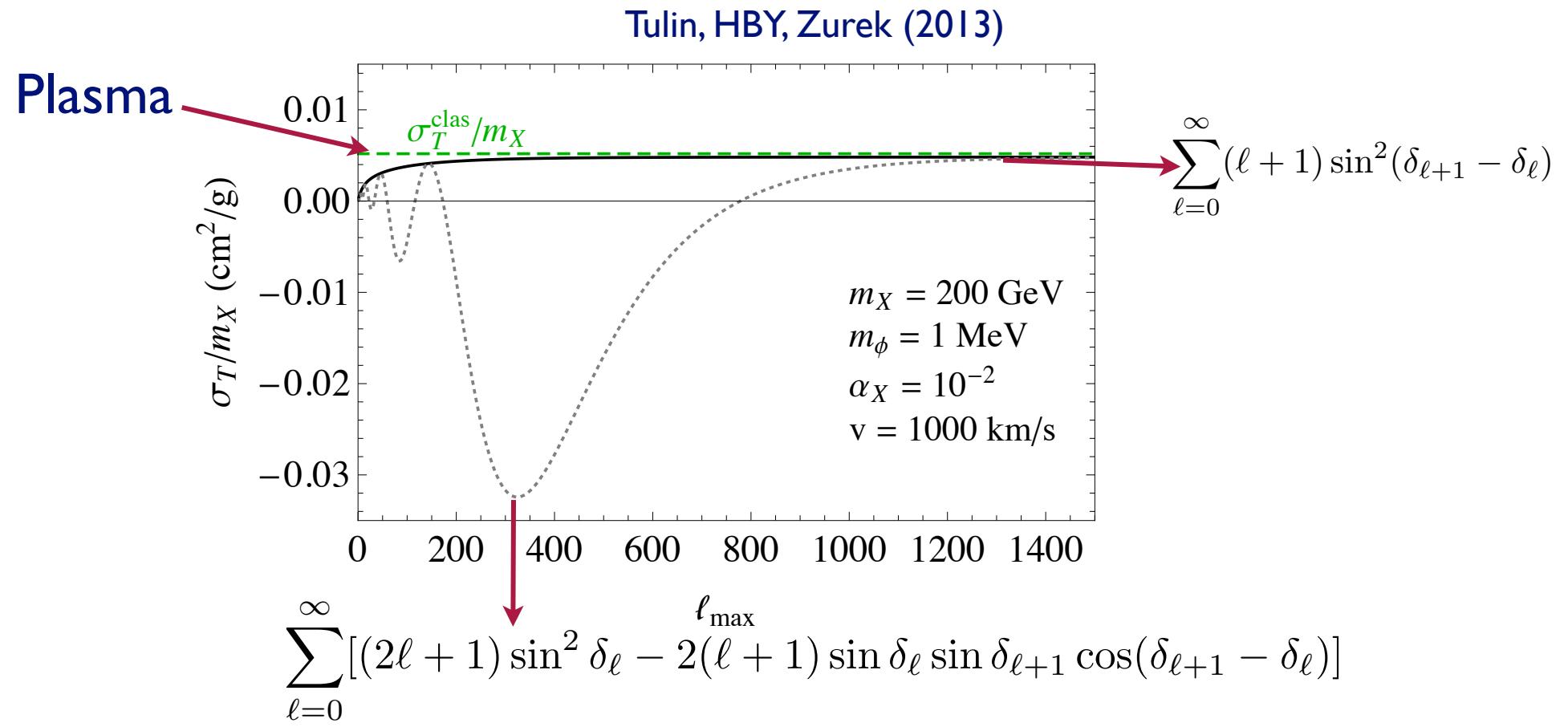
$$R_\ell(r) \rightarrow \cos \delta_\ell j_\ell(kr) - \sin \delta_\ell n_\ell(kr)$$



The second one is much more efficient

Numerical Approach

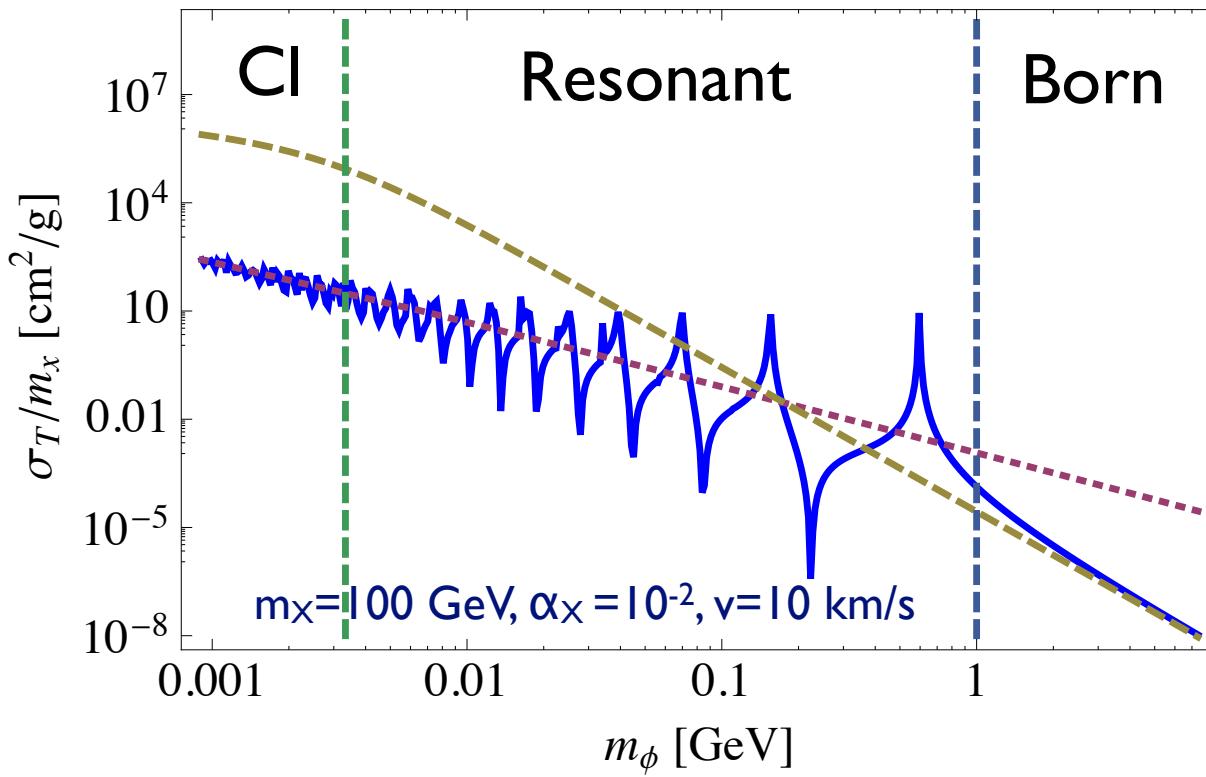
- Classical regime



We have confirmed the analytical formula from plasma physics

Numerical Approach

- All regimes



Solid: numerical; Dashed: Born; Dotted: plasma

In the resonant regime, the cross section can be enhanced or suppressed

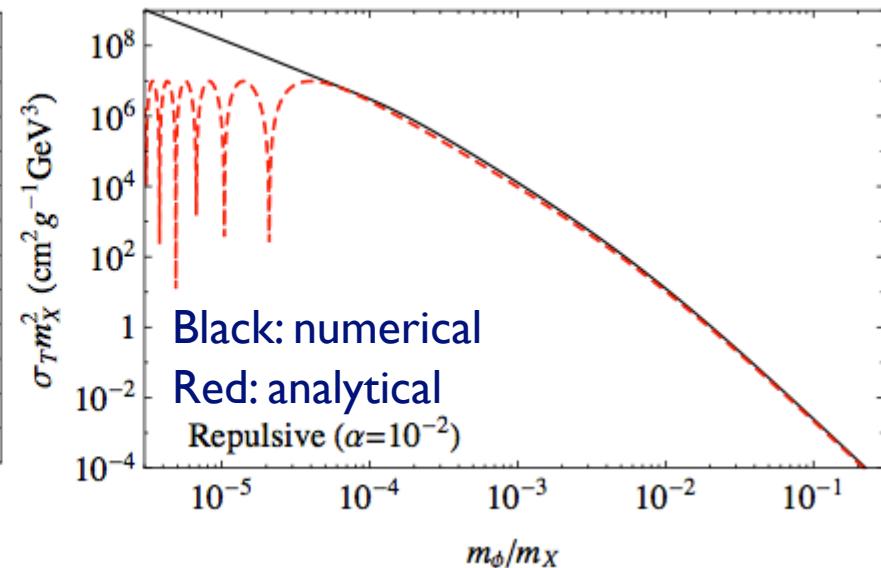
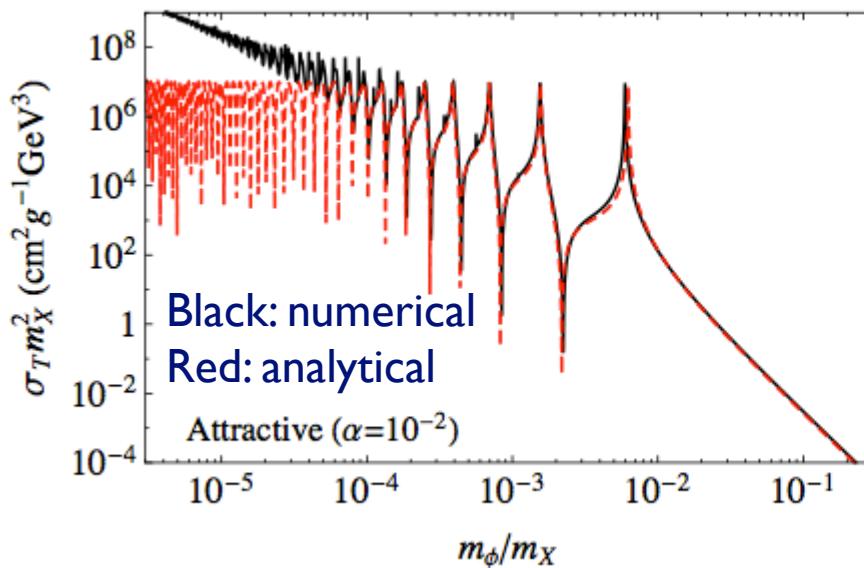
Analytical Approach

$$V(r) = \pm \frac{\alpha_X}{r} e^{-m_\phi r} \quad \longrightarrow \quad V(r) = \pm \frac{\alpha_X \delta e^{-\delta r}}{1 - e^{-\delta r}} \quad \begin{aligned} \delta &= \kappa m_\phi \\ \kappa &\simeq 1.6 \end{aligned}$$

Hulthén potential

The Schrödinger equation is solvable analytically for ell=0

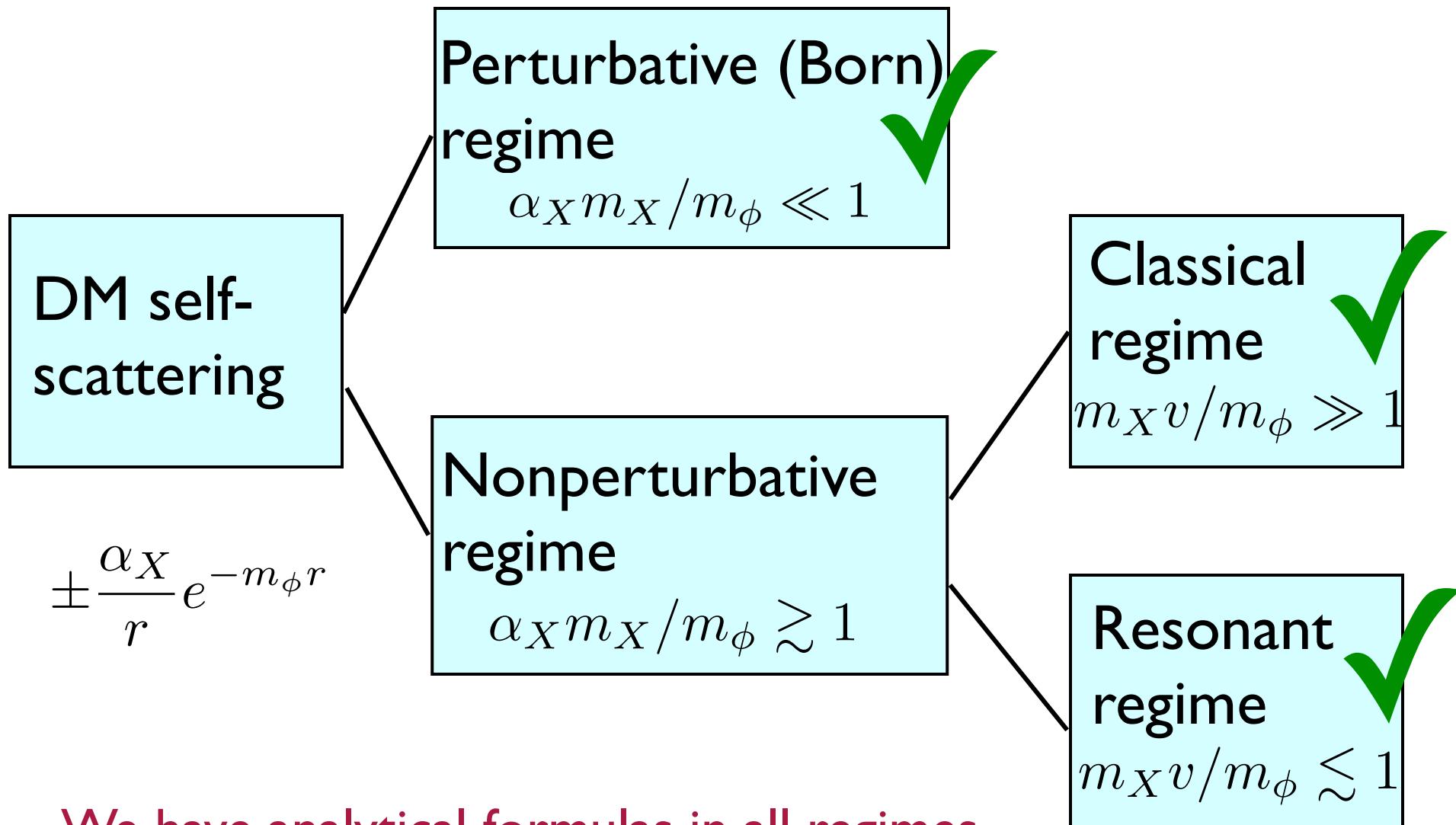
$$\sigma_T^{\text{Hulthén}} = \frac{16\pi}{m_X^2 v^2} \sin^2 \delta_0 \quad \delta_0 = \arg \left(\frac{i \Gamma(\frac{im_X v}{\kappa m_\phi})}{\Gamma(\lambda_+) \Gamma(\lambda_-)} \right), \quad \lambda_{\pm} \equiv \begin{cases} 1 + \frac{im_X v}{2\kappa m_\phi} \pm \sqrt{\frac{\alpha_X m_X}{\kappa m_\phi} - \frac{m_X^2 v^2}{4\kappa^2 m_\phi^2}} & \text{attractive} \\ 1 + \frac{im_X v}{2\kappa m_\phi} \pm i \sqrt{\frac{\alpha_X m_X}{\kappa m_\phi} + \frac{m_X^2 v^2}{4\kappa^2 m_\phi^2}} & \text{repulsive} \end{cases}$$



It is useful for simulations

Tulin, HBY, Zurek (2013)

Beyond Perturbation

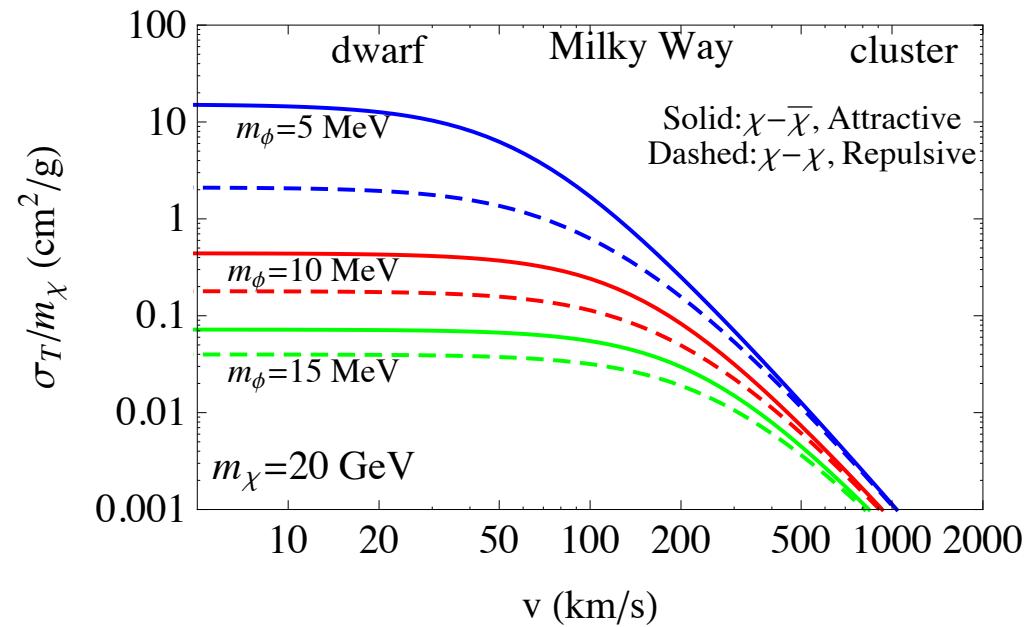
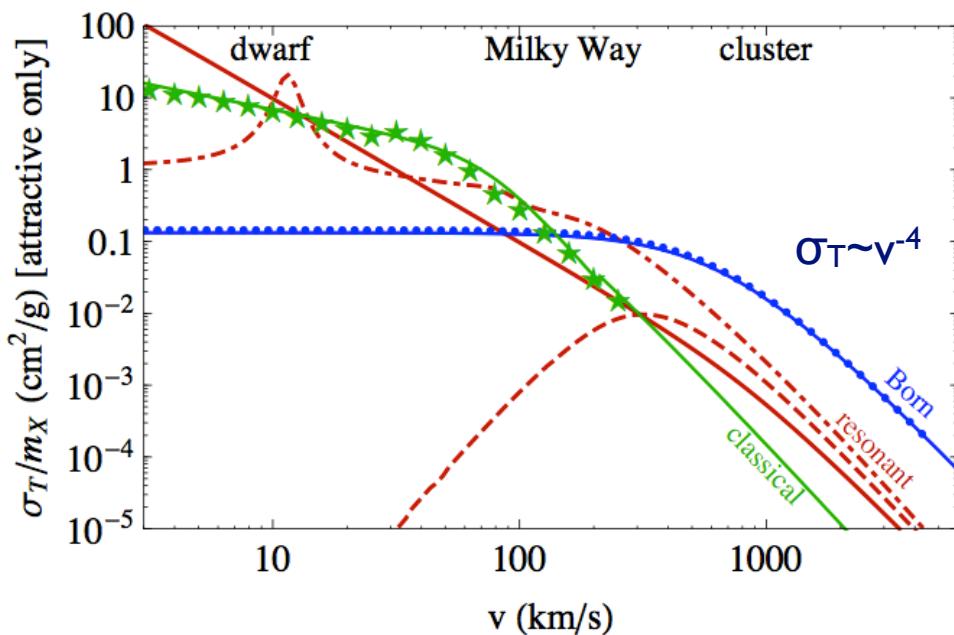


We have analytical formulas in all regimes

Velocity Dependence

- σ_T has rich structure

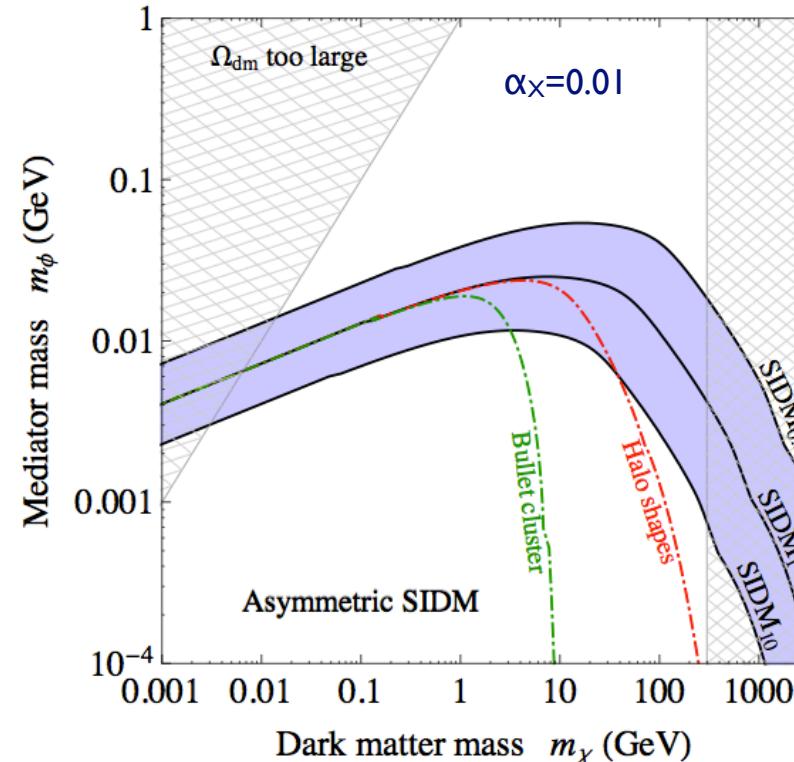
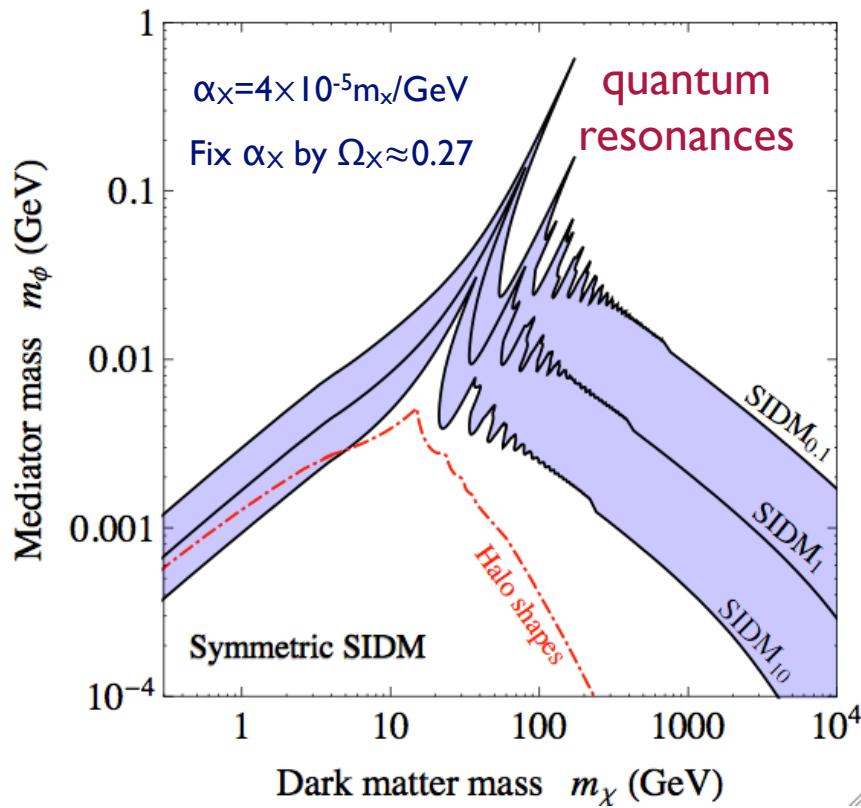
Tulin, HBY, Zurek (2011) (2012)



- In many cases, σ_T is enhanced on dwarf scales
- This helps us avoid constraints on cluster scales

SIDM Parameter Space

- Shaded region: Explain small scale anomalies



dw: dwarf (30 km/s); halo shapes: (300 km/s); cl: cluster (3000 km/s)

- SIDM predicts a 1-100 MeV light force carrier
- Bullet Cluster constraints are not sensitive to heavy SIDM

$$m_\chi \gg m_\phi$$

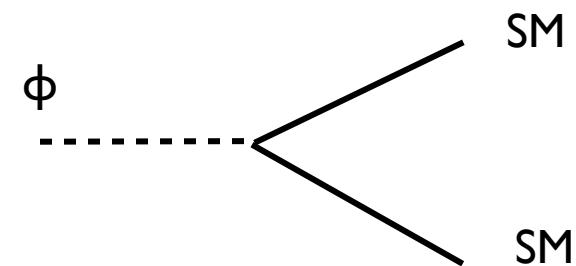
Cosmology of SIDM

- The mediator may dominate the energy density of the Universe
- The mediator decays before BBN: lifetime of ϕ is ~ 1 second

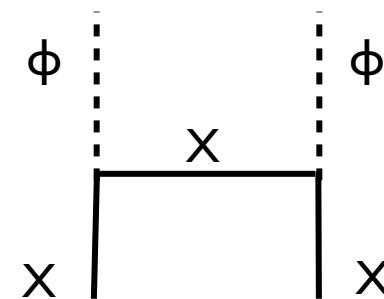
$$\epsilon \gtrsim 10^{-10} \sqrt{10 \text{ MeV}/m_\phi}$$

DD cross section:

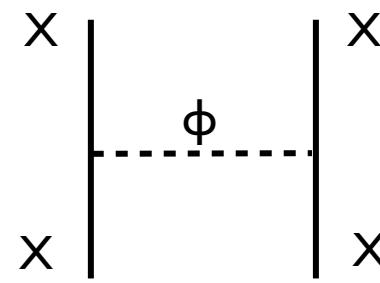
- suppressed by the tiny coupling
- enhanced by the small mediator mass



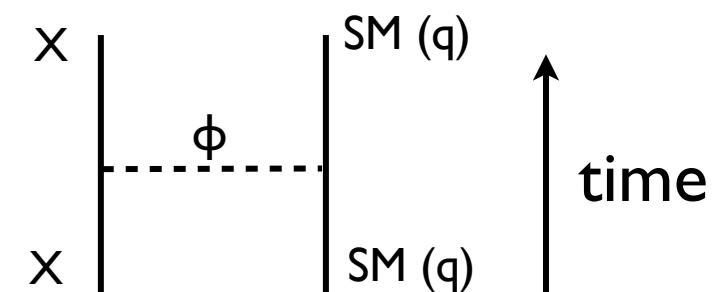
A super model!



DM relic density

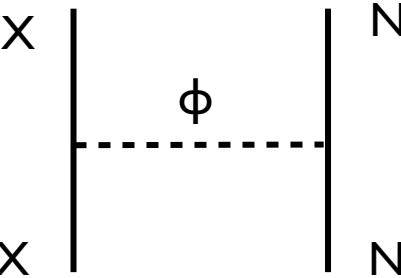


DM self-scattering



DM direct detection

Direct Detection of SIDM

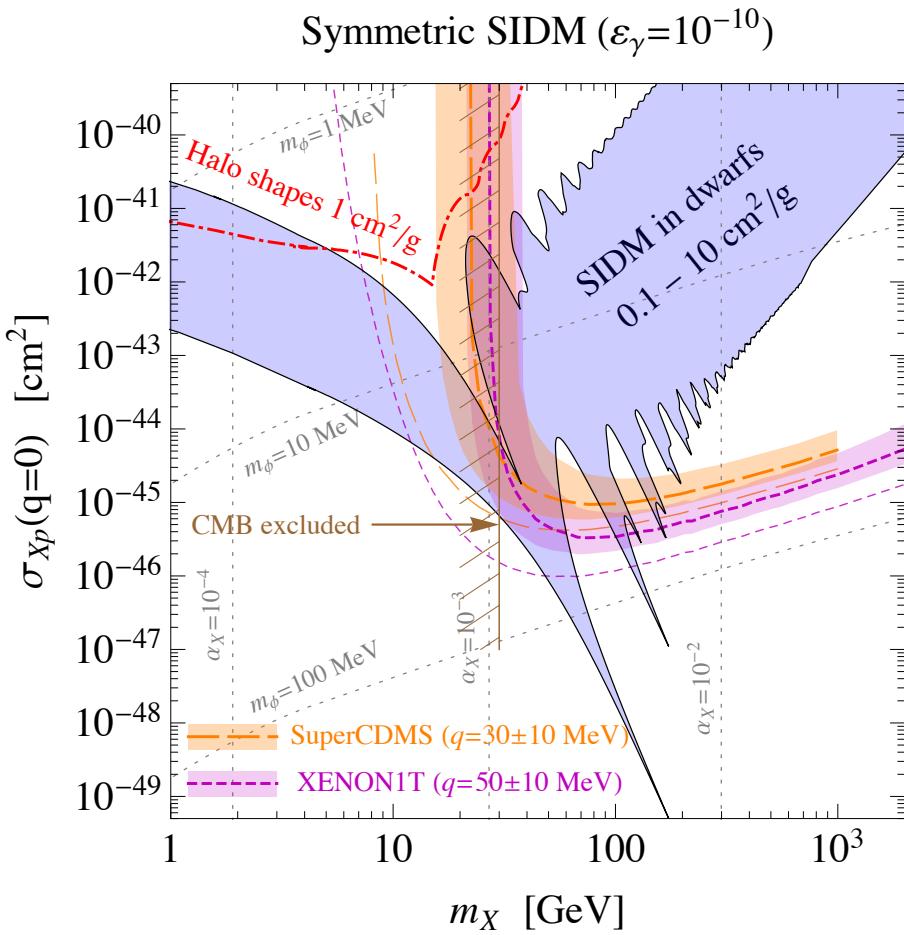

$$\frac{d\sigma}{dq^2} = \frac{4\pi\alpha_{em}\alpha_X\epsilon^2 Z^2}{(q^2 + m_\phi^2)^2 v^2}$$
$$q^2 = 2m_N E_R$$

For XENON: $q \sim 50$ MeV

- In the WIMP case, $m_\phi \gg q$
- For SIDM, $m_\phi \sim 1-100$ MeV, which is comparable to q
- A **NEW** region for the direct detection community
- A dedicated study is required

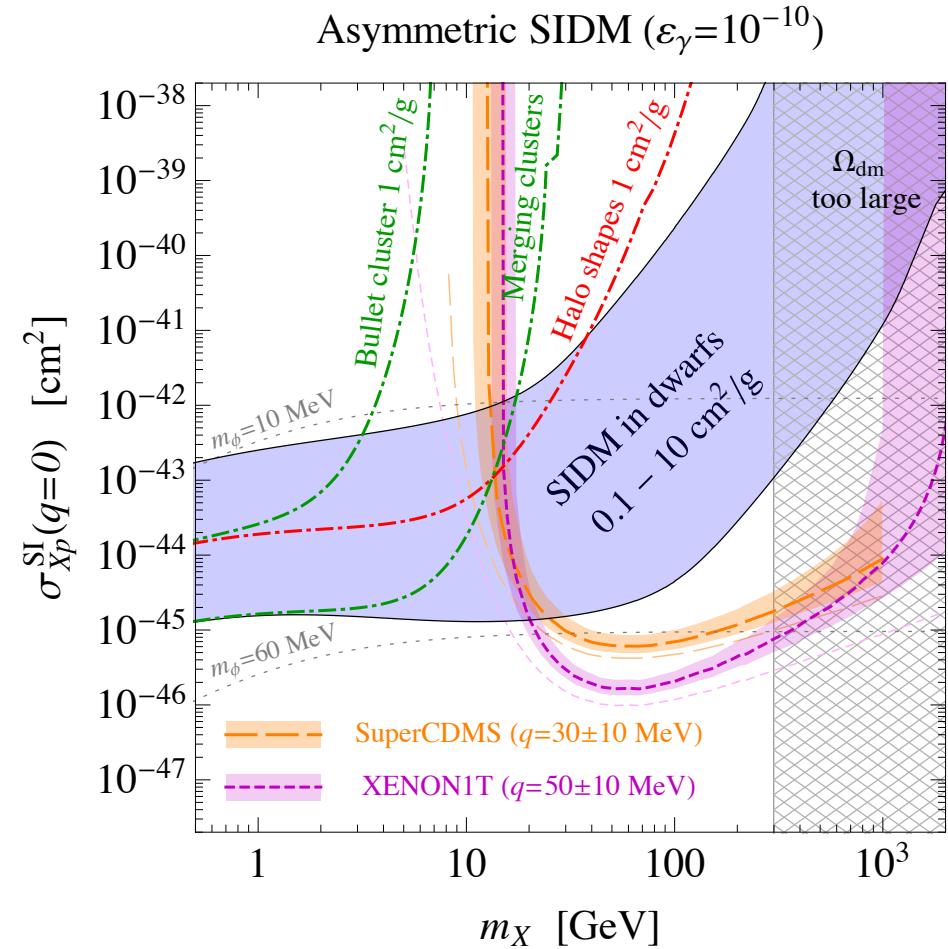
Direct Detection of SIDM

- The lower limit of direct detection cross section



$$\sigma_{Xp}^{\text{SI}} \approx 1.5 \times 10^{-24} \text{ cm}^2 \times \varepsilon_\gamma^2 \times \left(\frac{\alpha_X}{10^{-2}}\right) \left(\frac{m_\phi}{30 \text{ MeV}}\right)^{-4}$$

cross section in the zero momentum limit



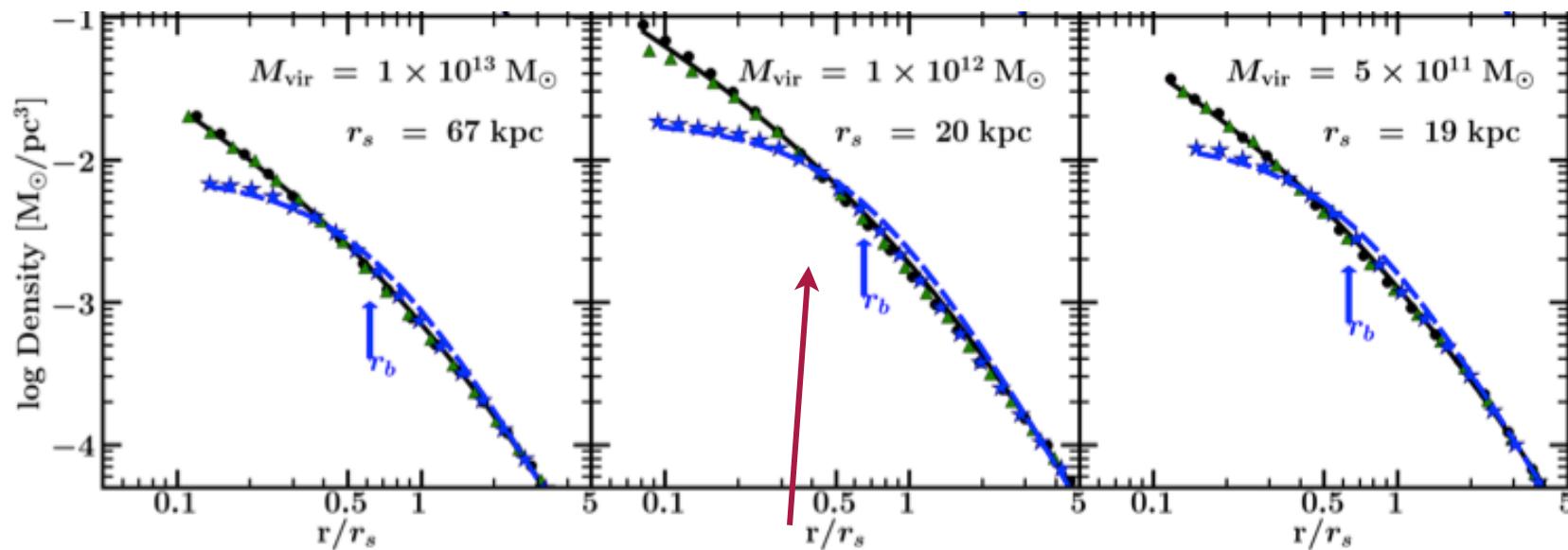
Kaplinghat, Tulin, HBY (2013)

Complementarity!

SIDM Profiles in Main Halos

- SIDM-only simulations

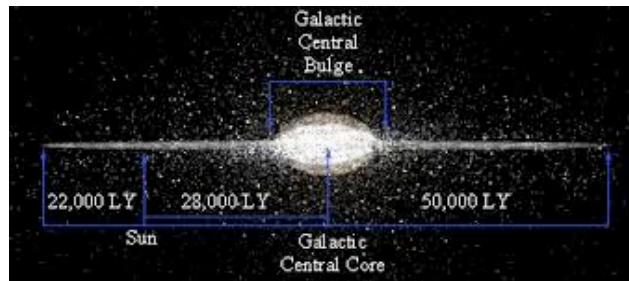
Rocha, Peter, Bullock, Kaplinghat, Garrison-Kimmel, Onorbe, Moustakas (2012)



MW-like main halos: the core size is about 10 kpc if $\sigma/m_X \sim 1 \text{ cm}^2/\text{g}$
Indirect detection signals would be very weak

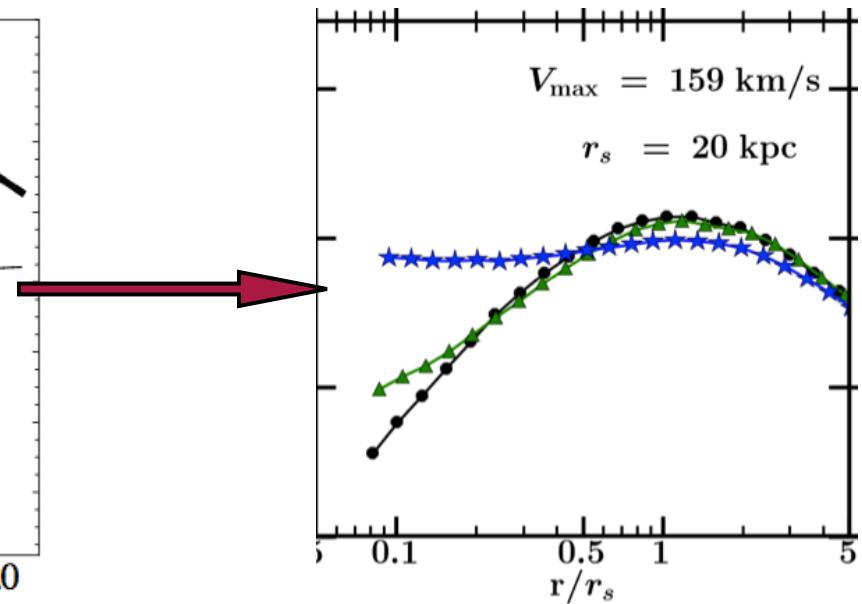
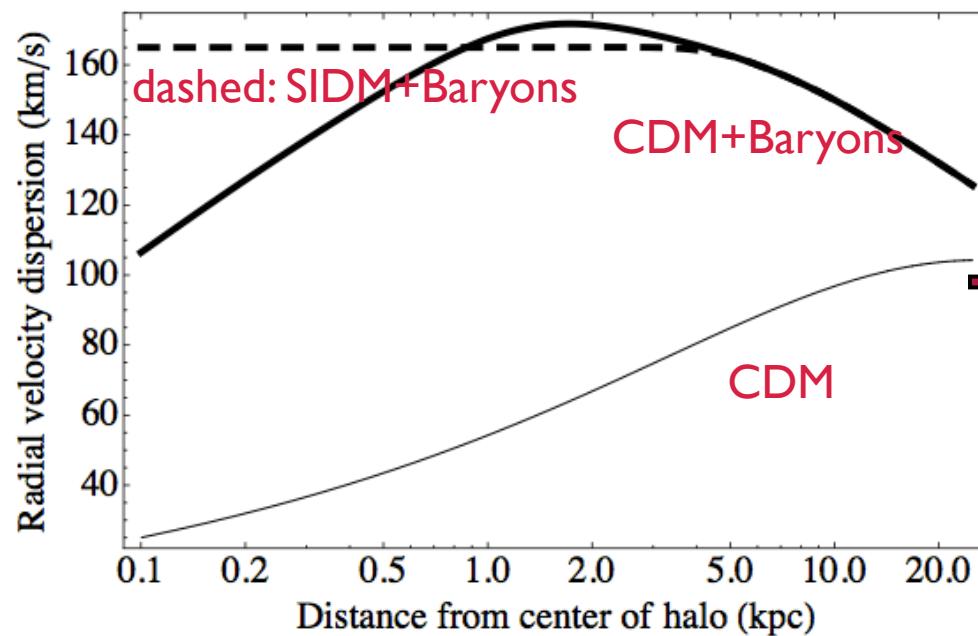
Tying Dark Matter to Baryons

- Baryons dominate in the central region of the Milky Way



Bulge: ~ 2 kpc

Kaplinghat, Linden, Keeley, HBY (2013)



Baryons dictate the DM temperature profile

SIDM Profiles with Baryons

- Baryons dominate in the central region of the Milky Way
isothermal solution for
the Jeans equation

$$\frac{\sigma^2}{\rho} \frac{d\rho}{dr} + \frac{d\sigma^2}{dr} = - \frac{d\Phi_B}{dr} - \frac{d\Phi}{dr}$$

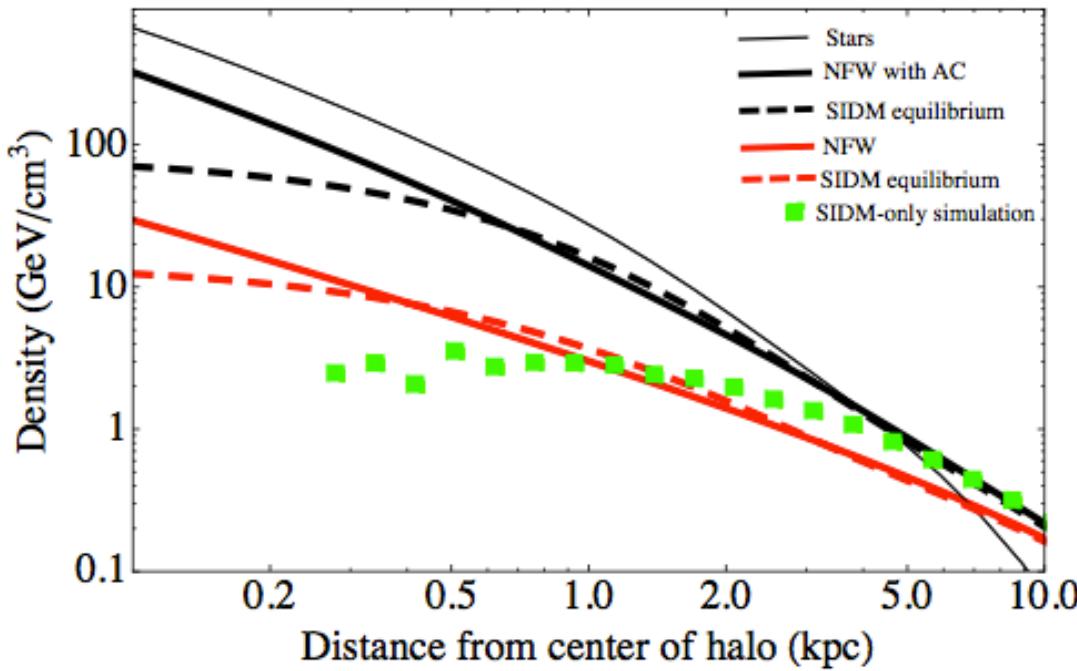
vanishes

σ, ρ_0 are unknown

SIDM and CDM have the same
total energy
total halo mass

The core size for the MW halo:
SIDM+baryons: $\sim 0.3\text{-}0.5$ kpc
SIDM only: core size ~ 10 kpc

Important for
indirect detection

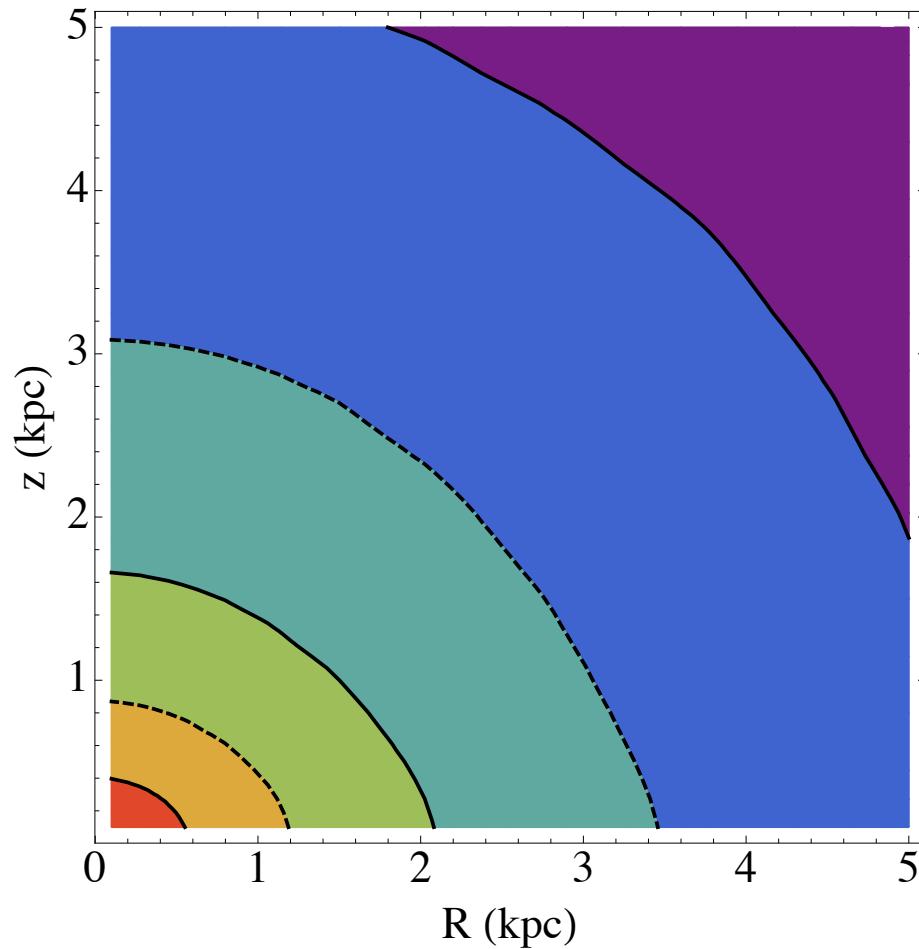


Kaplinghat, Linden, Keeley, HBY (2013)

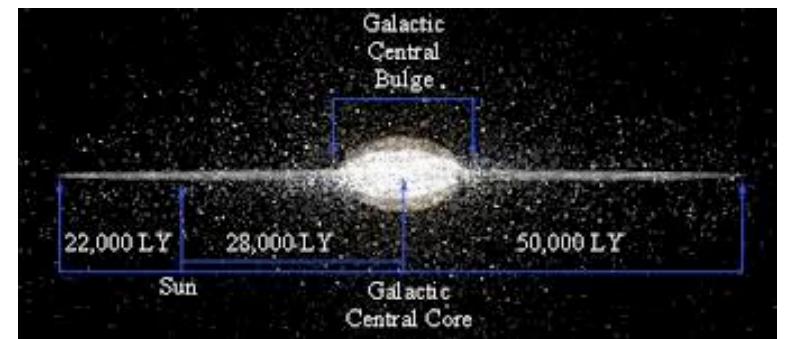
Halo Shapes with Baryons

- SIDM halo shapes

Kaplinghat, Linden, Keeley, HBY (2013)



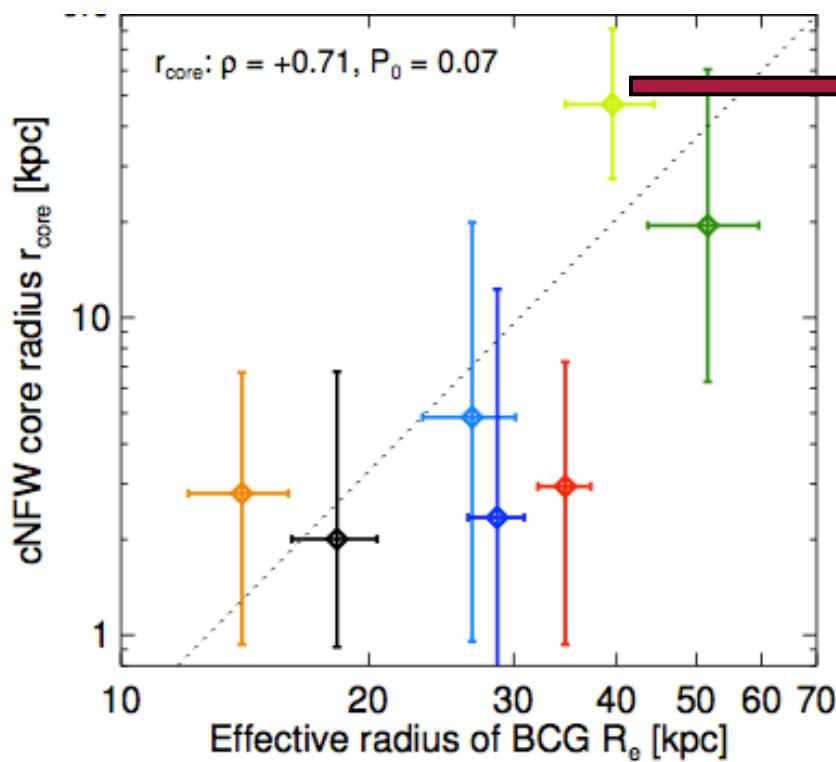
Constant density contours in cylindrical coordinates (R, z)



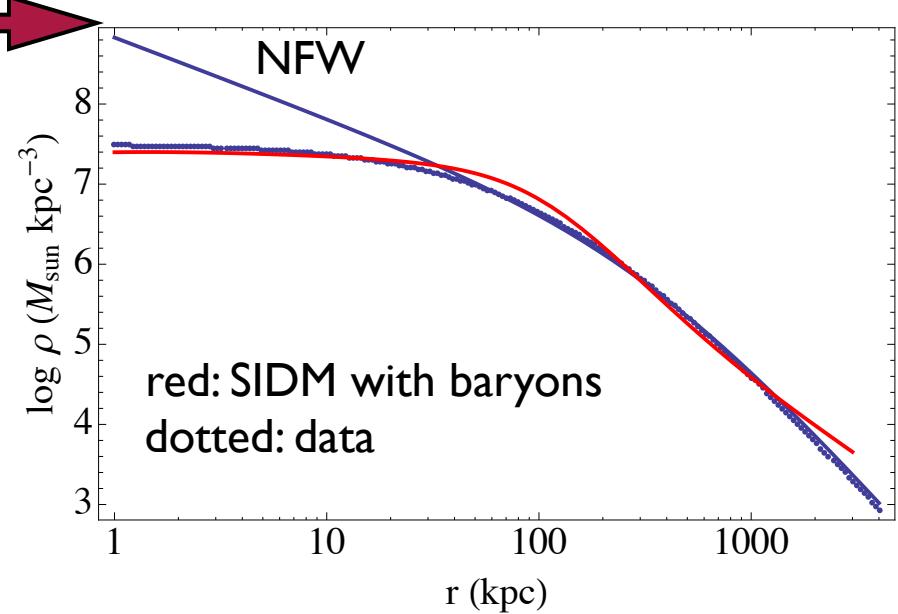
Rethink about halo shape constraints!

Tying Dark Matter to Baryons

- Cores in clusters



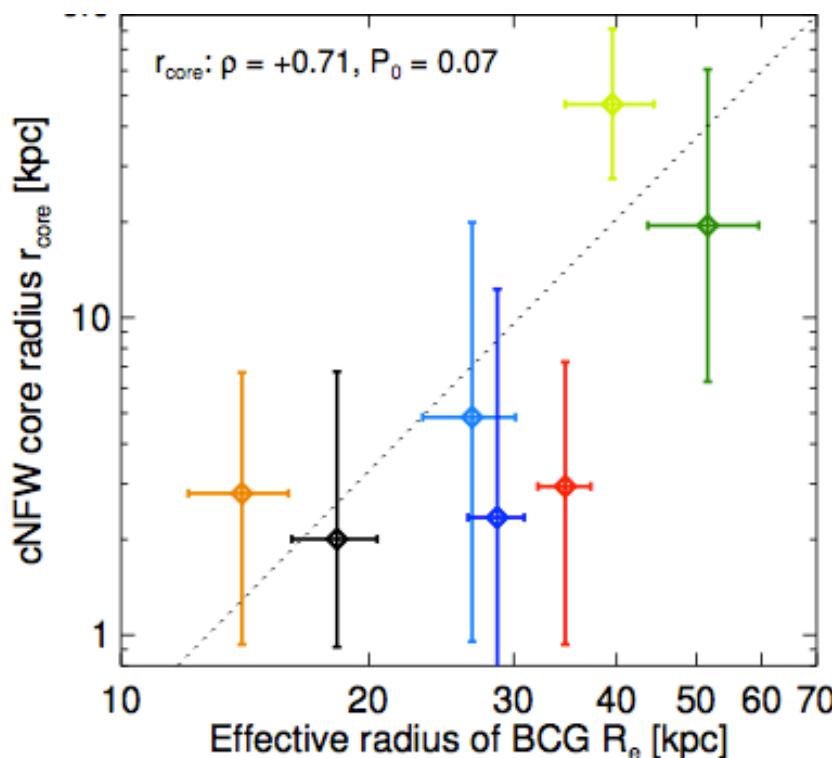
Newman, Treu, Ellis, Sand (2012)



Kaplinghat, HBY (work in progress)

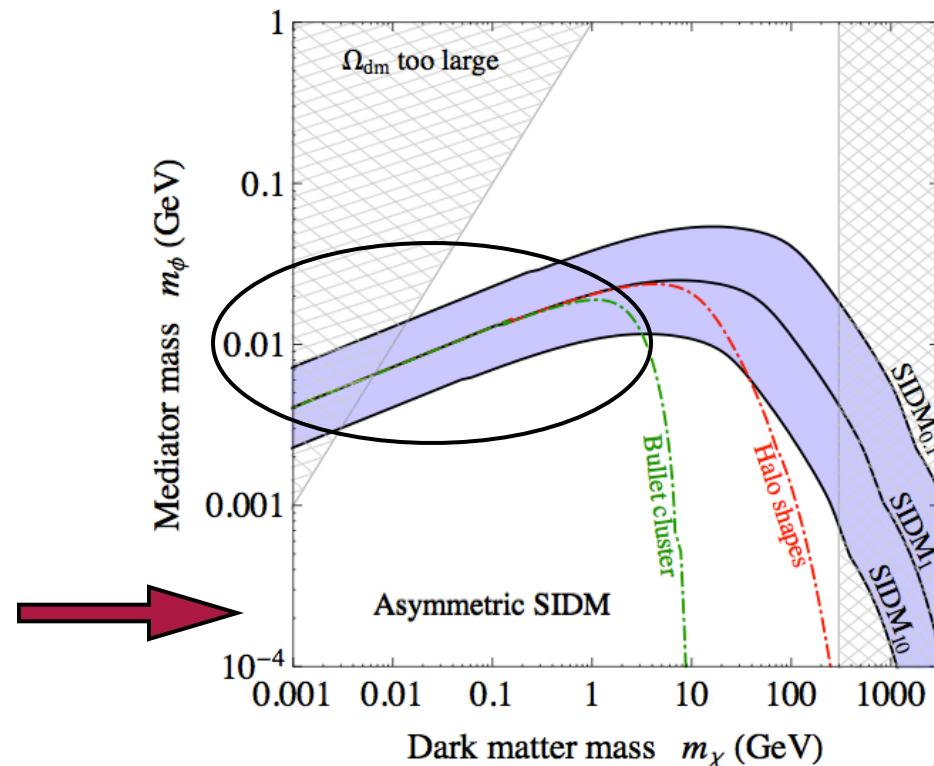
Tying Dark Matter to Baryons

- Cores in clusters



Newman, Treu, Ellis, Sand (2012)

Kaplinghat, HBY (work in progress)



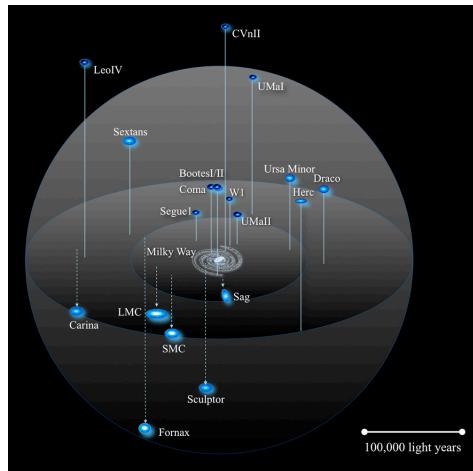
$m_\chi < m_\phi$ with $v \sim 800$ km/s

$m_\chi < 10 \text{ MeV}/(800 \text{ km/s}/c) \sim 4 \text{ GeV}$

Cores in clusters indicate light SIDM

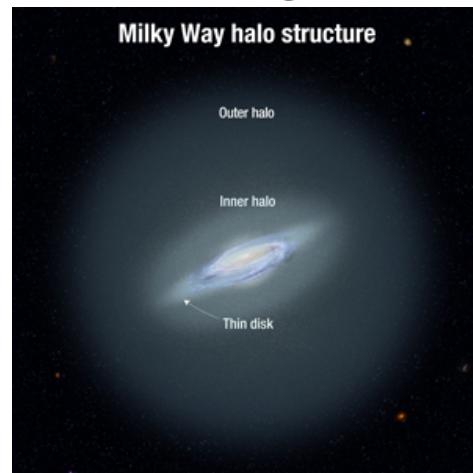
Dark Matter “Colliders”

Dwarf galaxies



“B-factory”

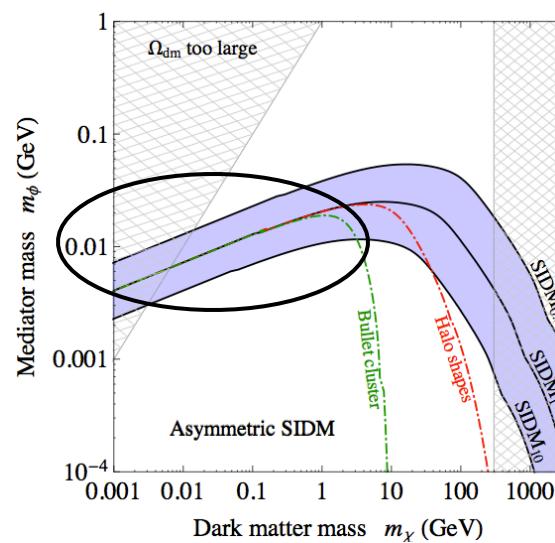
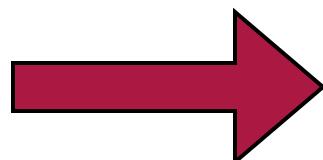
MW-size galaxies



Clusters



“LHC”



The dark sector
may not be as dark
as you thought

Conclusions

- No reason to believe DM has to be collisionless
- SIDM is an interesting alternative to CDM
- With a light dark force (with one coupling α_x)
 - Explain anomalies on small scales
 - Provide the correct DM relic density
 - Interesting direct detection signals
- Self-interactions ties DM to baryons

$$\Lambda\text{CDM} \longrightarrow \Lambda\text{SIDM}$$