

Neutralino WIMP dark matter

Varun Vaidya

Dept. of Physics, CMU

Los Alamos Natl. Lab

Based on the work with M. Baumgart and I.Z. Rothstein,

(PRL:114 (2015) 211301), M. Baumgart, I.Z. Rothstein, V.V

(JHEP:1504(2015) 106), M. Baumgart, I.Z. Rothstein, V.V

(ArXiv: 1510.02470), M. Baumgart and V.V

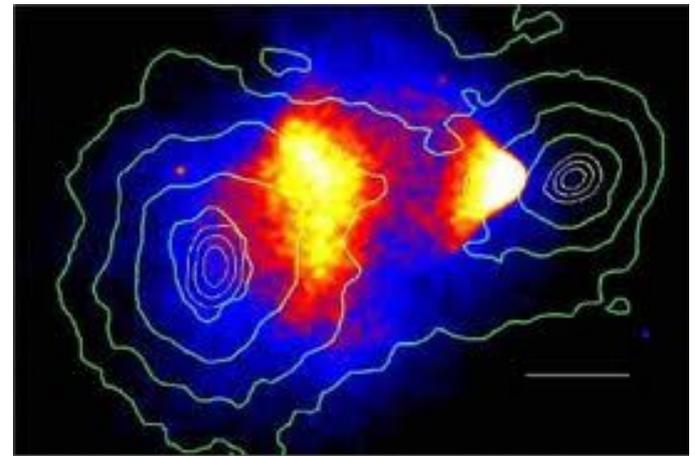
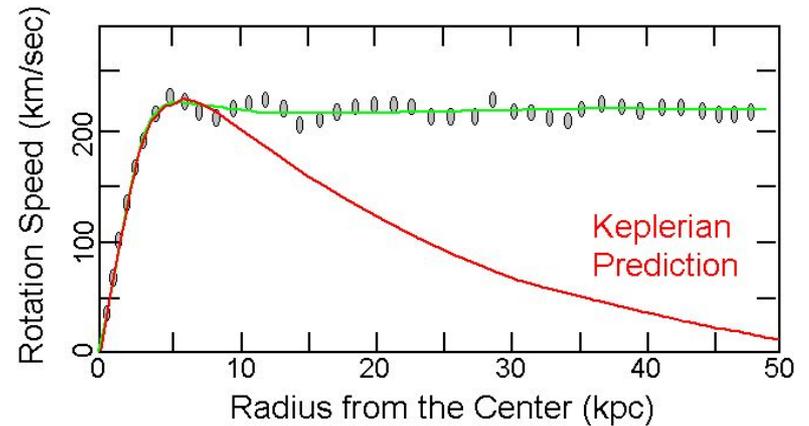
Outline

- Introduction to dark matter
- What are we calculating
- Why are we calculating what we are calculating
- How are we calculating it
- What do the calculations imply
- Summary and future work

Evidence for dark matter

- Rotation curves of galaxies
- Gravitational lensing from galactic clusters
- MACHO's?
- Cosmological evidence : Anisotropies in CMB are too small for observed structure
- Collision of Bullet cluster with cluster 1E 0657-56

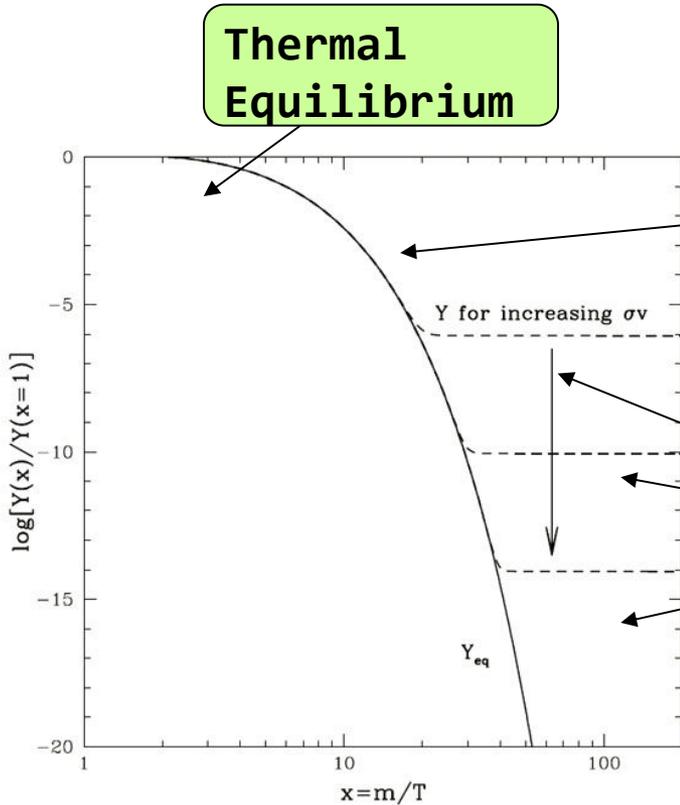
Observed vs. Predicted Keplerian



Dark Matter Candidates

- Massive particle that interacts gravitationally but only very weakly or not at all with SM particles (WIMP's)
- Neutrinos, Axions?
- Along came SUSY : naturalness problem, gauge coupling unification, natural dark matter candidate ->neutralino, sneutrino, gravitino?
- Neutralino : Massive cold dark matter, lightest supersymmetric partner(LSP) is stable by R parity conservation

The WIMP Miracle



Thermal Relic density

1. Expanding Universe
2. Net annihilation

Freeze -out, $\Gamma \sim H$

- Relic Abundance calculation using Boltzmann equation for a weakly interacting particle \sim TeV scale WIMP

$$M_X \sim \text{TeV} \left(10\sqrt{C\alpha} \right) \sqrt{\frac{\Omega_X h^2}{0.12}}$$

Assuming $\langle \sigma v \rangle \sim C\alpha^2/M_X^2$

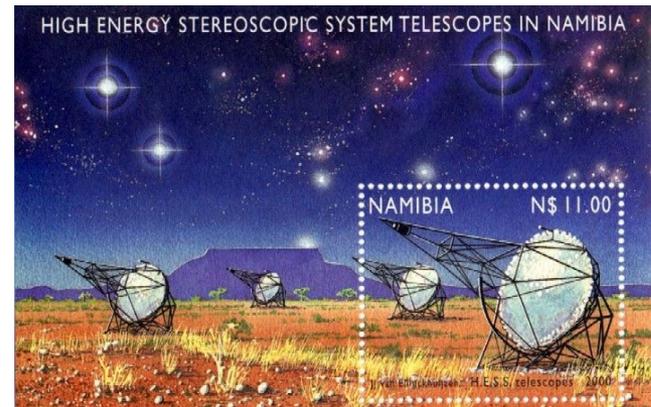
Direct detection

- Production at Colliders :LHC?
- Radioactively clean nuclei recoiling against a scattered DM particle: XENON, LUX ..

Indirect Detection

Goal: Detect Gamma Ray lines at WIMP mass

- Air Cherenkov Telescope :
HESS - High energy stereoscopic system ,
Namibia



What are we calculating

- Cold neutral dark matter at galactic center, $v \sim 10^{-3}$ interacting weakly.
- Assuming that fermionic WIMP constitute the dark matter of the universe , Mass \sim TeV
- We want: annihilation cross section of the dark matter to monochromatic gamma rays at the WIMP mass

$$\chi^0\chi^0 \rightarrow \gamma + X$$

- A semi-inclusive cross section to a single high energy photon

WINO Dark matter

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \bar{\chi} (i\not{D} + M_2) \chi$$

- $SU_L(2)$ triplet fermion χ , superpartner of weak gauge bosons, free mass parameter $M_2 \sim \text{TeV}$
- Mass eigenstates after electroweak breaking:

$$\chi^0 = \chi^3$$

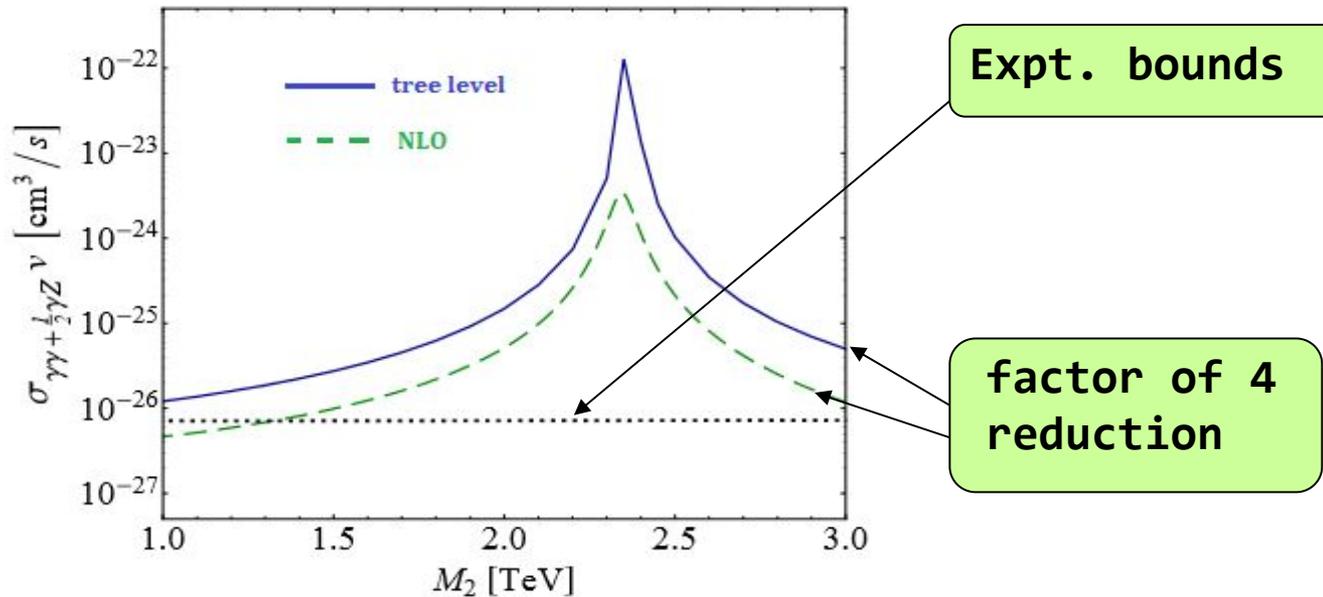
Neutralino : Majorana fermion

$$\chi^\pm = \frac{1}{\sqrt{2}}(\chi^1 \mp i\chi^2)$$

Chargino

- Mass splitting of 170 MeV from electroweak radiative corrections
- Neutral state χ^0 is the LSP \rightarrow Dark matter WINO

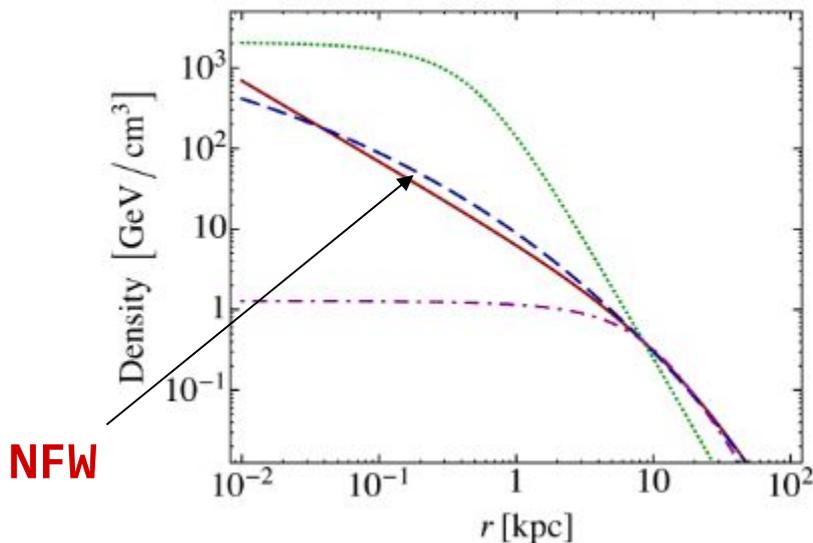
Wino Under Siege



- Previous results- fixed order, excludes the wino completely
- A suggestion that an NLO calculation can have a drastic impact on the cross section

Astronomical uncertainties

- Dark matter density ρ subject to large uncertainties
- A longstanding debate : Is the galactic DM halo cusped or cored?
- Flux of photons coming from Galactic center proportional to ρ^2



- A cored profile reduces the photon flux and hence can save the WINO

Imperative to have a good handle on theoretical errors

Exclusive vs Semi-inclusive

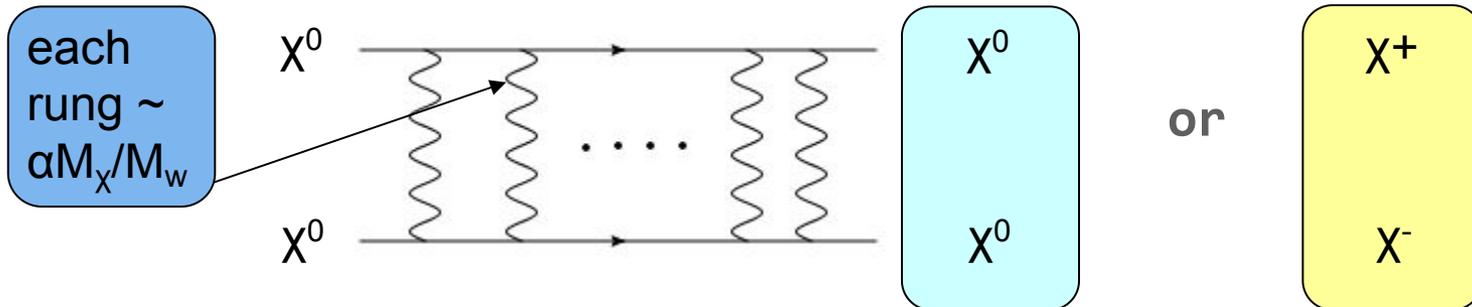
- Other complementary calculations : two body exclusive process $XX \rightarrow \gamma\gamma + 1/2\gamma Z$, an observed photon recoiling against an unseen photon or Z
- Missing channels in exclusive calculation :
 1. There is no restriction on the nature of recoil particles.
 2. The observed photon can be accompanied by soft radiation which lies below the detector energy resolution.
- Current detector resolution (HESS) $\sim 15\%$ of WIMP mass from 1-19 TeV. $\Rightarrow \Delta E > 150 \text{ GeV}$

Annihilation to photon

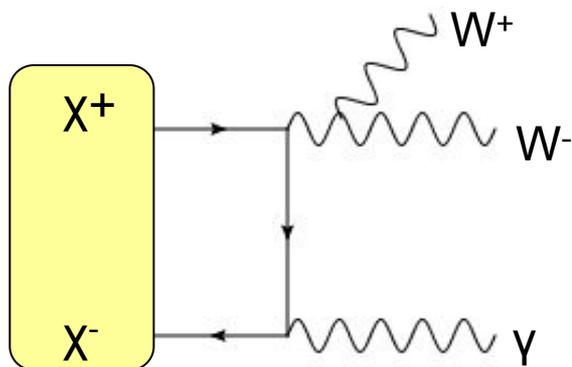
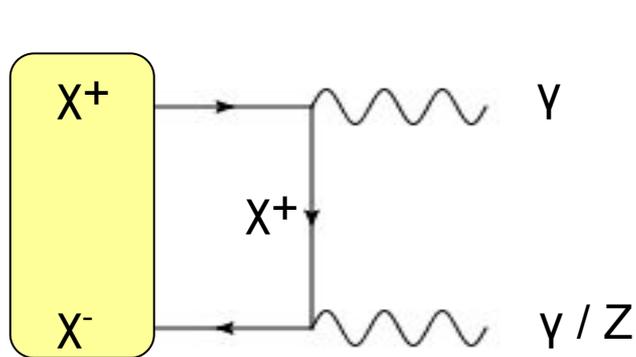
$$\chi^0 \chi^0 \rightarrow \gamma + X$$

- Semi- inclusive cross section of annihilation to a hard photon .
- The wino's are non relativistic , $v \sim 10^{-3}$
- Interaction has two contributions :

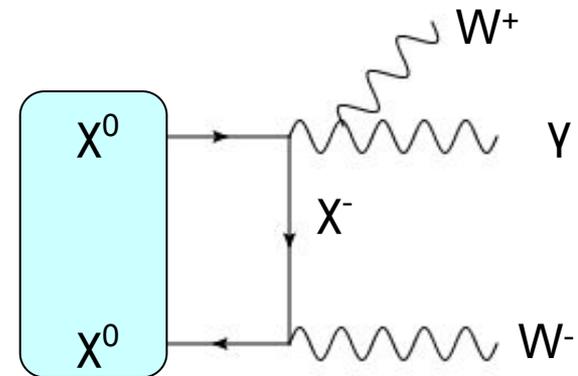
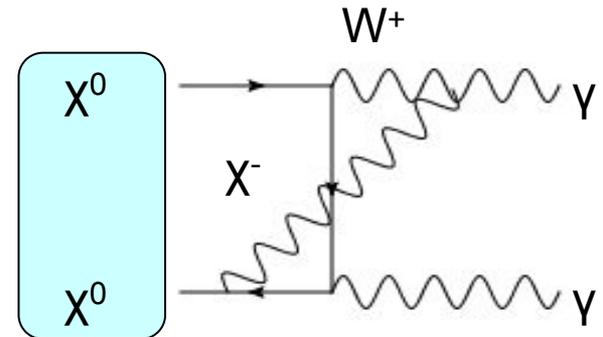
Phase 1 : Well separated ($r \sim 1/M_w$), slow moving fermions interact via gauge boson exchange



- Hard scattering at short distance ($r \sim 1/M_X$): Two channels available for semi-inclusive cross section



Chargino contribution begins at tree level



Neutralino only begins at one loop

Bloch Nordsieck violation

- IR safe observable -> final state should be a sum over indistinguishable (dangerous) states
- In Unbroken Electroweak theory, IR divergences due to semi-inclusive nature of cross section
- Gauge boson masses turn IR divergences to sudakov logs $\alpha_w \ln^2(M_X/M_W)$

$$\frac{\alpha_W}{\pi} \log(M_{\text{wino}}^2/m_W^2)^2 \approx 0.6$$

- Resummation becomes important to save perturbation theory.

EFT for WIMP Annihilation

- Factorize the long distance non perturbative physics from short distance annihilation process.

$$\frac{1}{E_\gamma} \frac{d\sigma}{dE_\gamma} = F_{00} |\psi_{00}(0)|^2 + F_{\pm} |\psi_{+-}(0)|^2 + F_{0\pm} (\psi_{00} \psi_{+-} + \text{h.c.})$$

$\psi_{00}(0)$, $\psi_{+-}(0)$ → Neutralino, Chargino two body wavefunction
enhancement factor due to long range gauge boson exchange

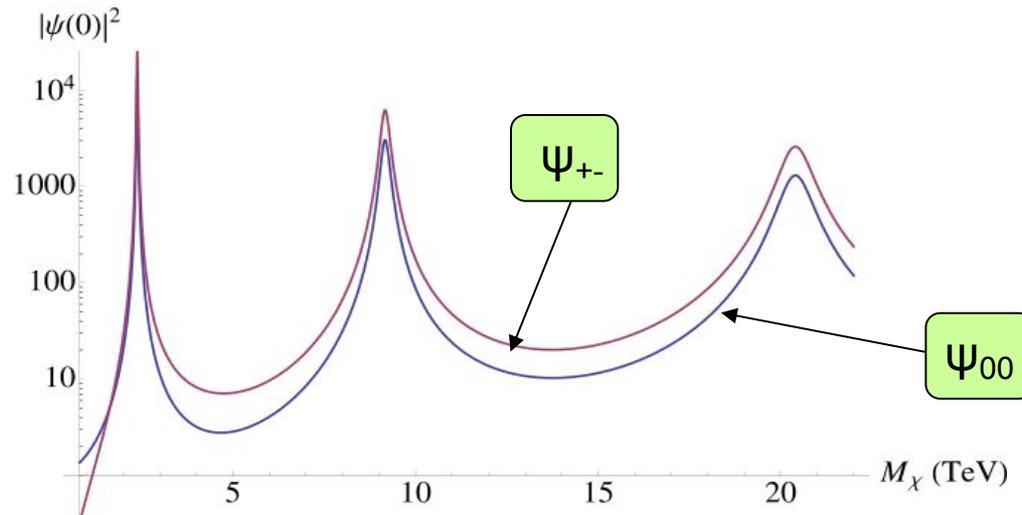
F_{00} , F_{\pm} , $F_{0\pm}$ → Short range hard annihilation to photon

Sommerfeld enhancement

- Effect captured by solving Schrodinger equation with effective potential

$$V(r) = \begin{pmatrix} 2\delta M - \frac{\alpha}{r} - \alpha_W c_W^2 \frac{e^{-m_Z r}}{r} & -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{r} \\ -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{r} & 0 \end{pmatrix}, \quad \psi = \begin{pmatrix} \Psi_{+-} \\ \Psi_{00} \end{pmatrix}$$

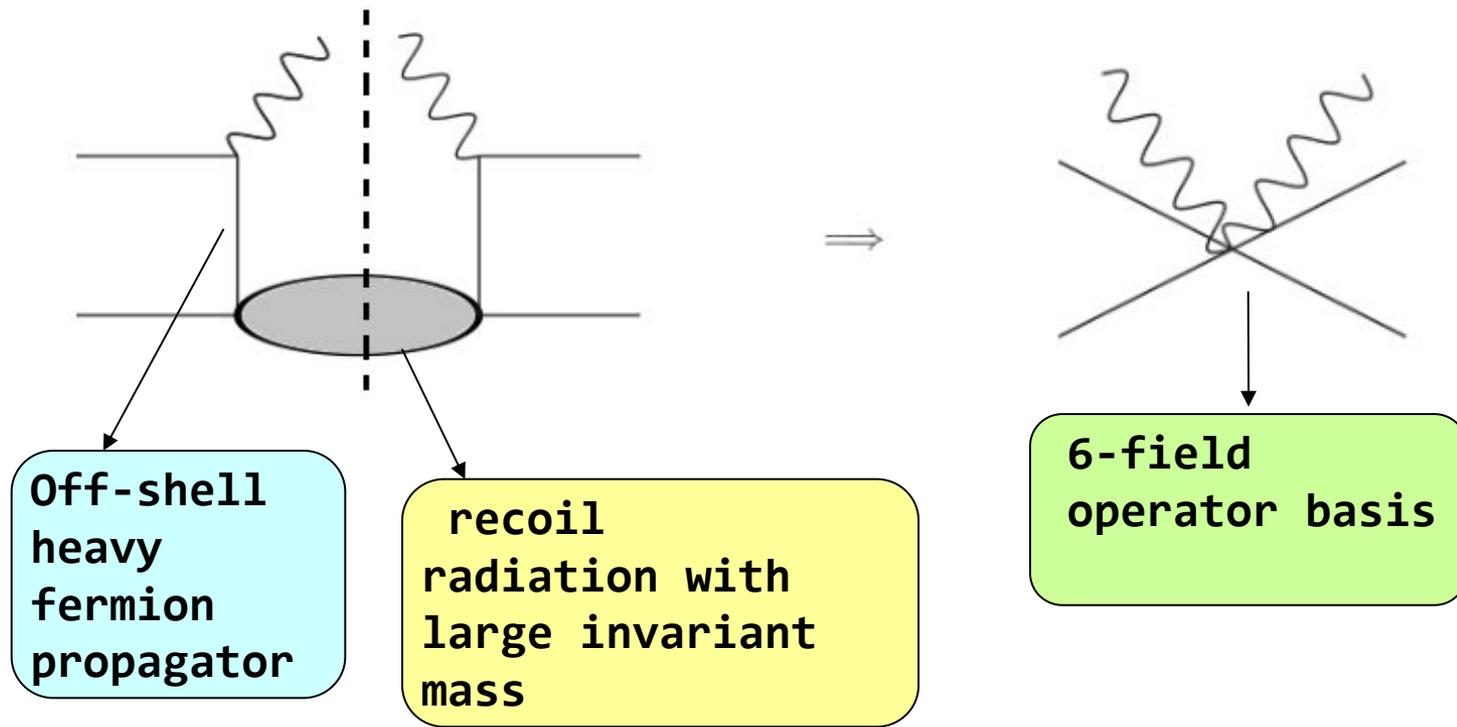
- Sommerfeld enhancement for two channels



EFT for annihilation

- Hybrid "NRQCD" - SCET II theory with expansion parameter $\lambda = M_W/M_X$

WIMP's	$\sim (E \sim \lambda^2, p \sim \lambda) \rightarrow$ Initial state	} NRQCD
Potential	$\sim (E \sim \lambda^2, p \sim \lambda) \rightarrow$ Long range Gauge boson exchange	
Collinear	$\sim (k^+ \sim 1, k^- \sim \lambda^2, k_\perp \sim \lambda) \rightarrow$ Final state photon + jet	} SCET
Soft	$\sim (k^+ \sim \lambda, k^- \sim \lambda, k_\perp \sim \lambda)$	



- Soft gauge invariance fixes the position of soft wilson lines required to reproduce IR physics
- Majorana condition reduces the operator basis to 4

$$O_1 = (\bar{\chi}\gamma^5\chi)(\bar{\chi}\gamma^5\chi) B^A B^A$$

$$O_3 = (\bar{\chi}_C\gamma^5\chi_D)(\bar{\chi}_D\gamma^5\chi_C) B^A B^A$$

$$O_2 = \frac{1}{2} \left\{ (\bar{\chi}\gamma^5\chi)(\bar{\chi}_{A'}\gamma^5\chi_{B'}) + (\bar{\chi}_{A'}\gamma^5\chi_{B'}) (\bar{\chi}\gamma^5\chi) \right\} B^{\tilde{A}} B^{\tilde{B}} S_{vA'A}^\top S_{vBB'} S_{n\tilde{A}\tilde{A}}^\top S_{nB\tilde{B}}$$

$$O_4 = (\bar{\chi}_{A'}\gamma^5\chi_C)(\bar{\chi}_C\gamma^5\chi_{B'}) B^{\tilde{A}} B^{\tilde{B}} S_{vA'A}^\top S_{vBB'} S_{n\tilde{A}\tilde{A}}^\top S_{nB\tilde{B}}$$

**Color-singlet
collinear sector ,
Trivial soft sector**

SCET building blocks

$$B^A B^B \equiv \sum_X B_\mu^{\perp A} |\gamma + X\rangle \langle \gamma + X| B^{\mu B \perp}$$

$$(\bar{\chi}_{A'}\gamma^5\chi_C)(\bar{\chi}_C\gamma^5\chi_{B'}) \equiv (\bar{\chi}_{A'}\gamma^5\chi_C)|0\rangle\langle 0|(\bar{\chi}_C\gamma^5\chi_{B'})$$

$$B_\mu^{\perp A} \equiv f^{ABC} W_n^T (D_\mu^\perp)^{BC} W_n$$

$$W_n^{BC} = P(e^g \int_{-\infty}^0 n \cdot A_n^A(n\lambda) f^{ABC} d\lambda)$$

$$S_{(v,n)bc} = P[e^g \int_{-\infty}^0 (v,n) \cdot A^a((v,n)\lambda) f^{abc} d\lambda]$$

Cross section :

$$\begin{aligned}
 \frac{1}{E_\gamma} \frac{d\sigma}{dE_\gamma} &= \frac{1}{4M_X^2 v} \langle 0 | O_s^a | 0 \rangle \left[\int dn \cdot p \left\{ C_2(M_X, n \cdot p) \langle p_1 p_2 | \frac{1}{2} \left\{ (\bar{\chi} \gamma^5 \chi) (\bar{\chi}_{A'} \gamma^5 \chi_{B'}) \right. \right. \right. \\
 &+ (\bar{\chi}_{A'} \gamma^5 \chi_{B'}) (\bar{\chi} \gamma^5 \chi) \left. \left. \left. \right\} (0) | p_1 p_2 \rangle + C_4(M_X, n \cdot p) \langle p_1 p_2 | (\bar{\chi}_{A'} \gamma^5 \chi_C) (\bar{\chi}_C \gamma^5 \chi_{B'}) (0) | p_1 p_2 \rangle \right\} F_{\tilde{A}\tilde{B}}^\gamma \left(\frac{2E_\gamma}{n \cdot p} \right) \right] \\
 &+ \left[\int dn \cdot p \left\{ C_1(M_X, n \cdot p) \langle p_1 p_2 | (\bar{\chi} \gamma^5 \chi) (\bar{\chi} \gamma^5 \chi) (0) | p_1 p_2 \rangle + C_3(M_X, n \cdot p) \right. \right. \\
 &\times \left. \left. \langle p_1 p_2 | (\bar{\chi}_C \gamma^5 \chi_D) (\bar{\chi}_D \gamma^5 \chi_C) (0) | p_1 p_2 \rangle \right\} F_\gamma \left(\frac{2E_\gamma}{n \cdot p} \right) \right],
 \end{aligned}$$

$$\begin{aligned}
 F_{\tilde{A}\tilde{B}}^\gamma \left(\frac{n \cdot k}{n \cdot p} \right) &= \int \frac{dx_-}{2\pi} e^{in \cdot p x_-} \langle 0 | B_{\tilde{A}}^{\perp \mu}(x_-) | \gamma(k_n) + X_n \rangle \\
 &\times \langle \gamma(k_n) + X_n | B_{\tilde{B}}^{\perp \mu}(0) | 0 \rangle,
 \end{aligned}$$

$$F_\gamma = F_{\tilde{A}\tilde{B}}^\gamma \delta_{\tilde{A}\tilde{B}}$$

Fragmentation functions

$$O_s^a = S_{vA'A}^T S_{vBB'} S_{n\tilde{A}\tilde{A}}^T S_{nB\tilde{B}}$$

$$O_s^b = \mathbb{1} \delta_{\tilde{A}\tilde{B}} \delta_{A'B'}$$

Soft Operators

$$O_c^a = B_{\tilde{A}}^\perp | \gamma(k_n) + X_n \rangle \langle \gamma(k_n) + X_n | B_{\tilde{B}}^\perp$$

$$O_c^b = B_{\tilde{D}}^\perp | \gamma(k_n) + X_n \rangle \langle \gamma(k_n) + X_n | B_{\tilde{D}}^\perp \delta_{\tilde{A}\tilde{B}}$$

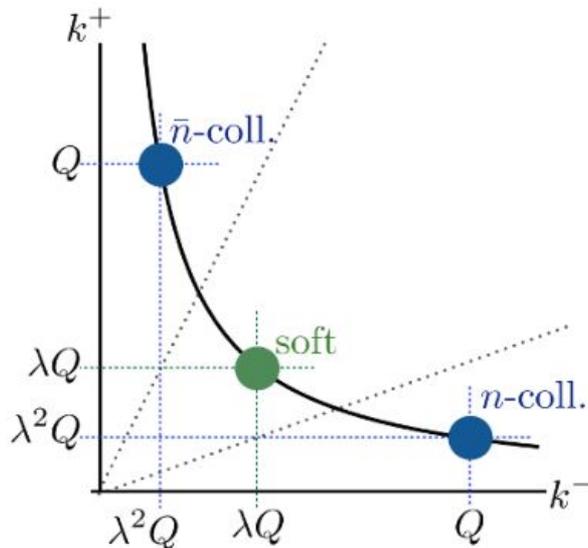
Collinear Operators

Rapidity renormalization group

$$\mu \frac{d}{d\mu} \begin{pmatrix} O_a^{c,s} \\ O_b^{c,s} \end{pmatrix} = \begin{pmatrix} \gamma_{\mu,aa}^{c,s} & \gamma_{\mu,ab}^{c,s} \\ \gamma_{\mu,ba}^{c,s} & \gamma_{\mu,bb}^{c,s} \end{pmatrix} \begin{pmatrix} O_a^{c,s} \\ O_b^{c,s} \end{pmatrix}$$

$$\nu \frac{d}{d\nu} \begin{pmatrix} O_a^{c,s} \\ O_b^{c,s} \end{pmatrix} = \begin{pmatrix} \gamma_{\nu,aa}^{c,s} & \gamma_{\nu,ab}^{c,s} \\ \gamma_{\nu,ba}^{c,s} & \gamma_{\nu,bb}^{c,s} \end{pmatrix} \begin{pmatrix} O_a^{c,s} \\ O_b^{c,s} \end{pmatrix}$$

Rapidity renormalization group equations



New divergences due to Factorization: usually regulated by dim. reg.

Rapidity divergences due to separation of the soft and collinear regions: a new regulator is needed that breaks residual boost invariance

Anomalous Dimensions

$$\begin{aligned} \gamma_{\mu,aa}^c &= \frac{3\alpha_W}{\pi} \log\left(\frac{\nu^2}{4M_\chi^2}\right) + \frac{\alpha_W}{2\pi} \left(\beta_0 - 2 \int_{z_{cut}}^1 dz P_{gg}^*(z) \right), \\ \gamma_{\mu,ab}^c &= -\frac{\alpha_W}{\pi} \log\left(\frac{\nu^2}{4M_\chi^2}\right) + \frac{\alpha_W}{\pi} \int_{z_{cut}}^1 dz P_{gg}^*(z), \\ \gamma_{\mu,bb}^c &= \frac{\alpha_W}{\pi} \left(\frac{\beta_0}{2} + 2 \int_{z_{cut}}^1 dz P_{gg}^*(z) \right). \end{aligned}$$

One loop Cusp

One loop non-cusp

- Operator mixing in each sector for μ and ν anomalous dimensions.

$$\begin{aligned} \gamma_{\mu,aa}^s &= -\frac{3\alpha_W}{\pi} \log\left(\frac{\nu^2}{\mu^2}\right) + \frac{3\alpha_W}{\pi}, \\ \gamma_{\mu,ab}^s &= \frac{\alpha_W}{\pi} \log\left(\frac{\nu^2}{\mu^2}\right) - \frac{\alpha_W}{\pi}. \end{aligned}$$

$$\begin{aligned} \gamma_{\nu,aa}^c &= \frac{3\alpha_W}{\pi} \log\left(\frac{\mu^2}{M_W^2}\right), & \gamma_{\nu,aa}^s &= -\frac{3\alpha_W}{\pi} \log\left(\frac{\mu^2}{M_W^2}\right), \\ \gamma_{\nu,ab}^c &= -\frac{\alpha_W}{\pi} \log\left(\frac{\mu^2}{M_W^2}\right), & \gamma_{\nu,ab}^s &= \frac{\alpha_W}{\pi} \log\left(\frac{\mu^2}{M_W^2}\right). \end{aligned}$$

$$P_{gg}^*(z) = 2 \left[z(1-z) + \frac{z}{(1-z)^+} + \frac{1-z}{z} \right]$$

- ν anomalous dimension cancels between soft and collinear sectors.

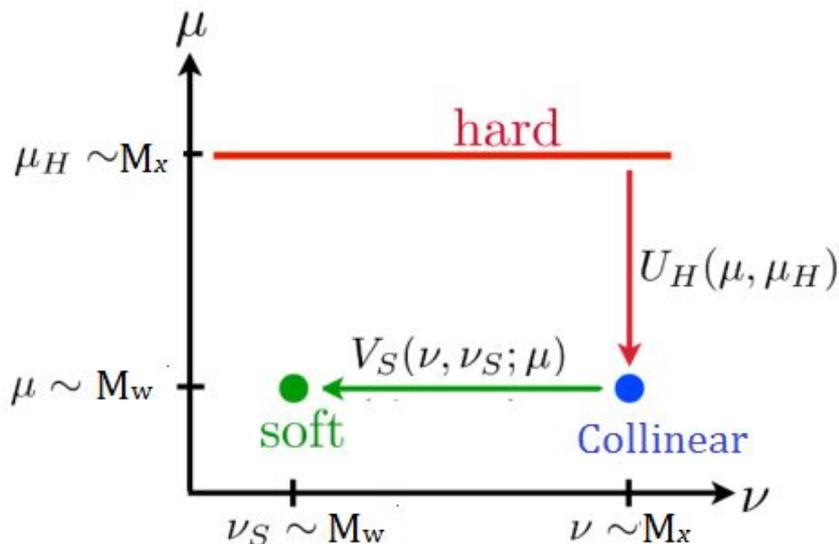
Resummation at LL'

Power counting at LL' :

$\alpha_w \ln^2(M_X/M_W) \sim 1$ resummed to all orders,

$\alpha_w \ln(M_X/M_W) \ll 1$, included only at leading order

Net result: All terms of the form $\alpha_w^{n+1} \ln^{2n+1}(M_X/M_W)$



Resummation of logs by
choosing a path in μ, ν
space

Total rate

- Resummed cross section

$$\sigma v = \frac{\pi \alpha_W^2 \sin^2 \theta_W}{8M_\chi^4} \left\{ \frac{4}{3} f'_- |\psi_{00}(0)|^2 + 4f'_+ |\psi_{\pm}(0)|^2 + \frac{4}{3} f'_- (\psi_{00}(0)\psi_{\pm}^*(0) + \text{h.c.}) \right\},$$

Ψ_{00}, Ψ_{+-} \longrightarrow Sommerfeld enhancement factors

Sudakov factors

$$f'_{\pm} = (1 \pm E_1) + (LP_g + \Pi_{\gamma\gamma}) \pm E_1 (P'_g L + \Pi_{\gamma\gamma}) \mp 2E_1 \frac{\alpha_W}{\pi} L^2 \left(\frac{\alpha_W}{2\pi} \beta_0 L + \Pi_{\gamma\gamma} \right).$$

$\Pi_{\gamma\gamma}$ \longrightarrow photon self energy at M_W

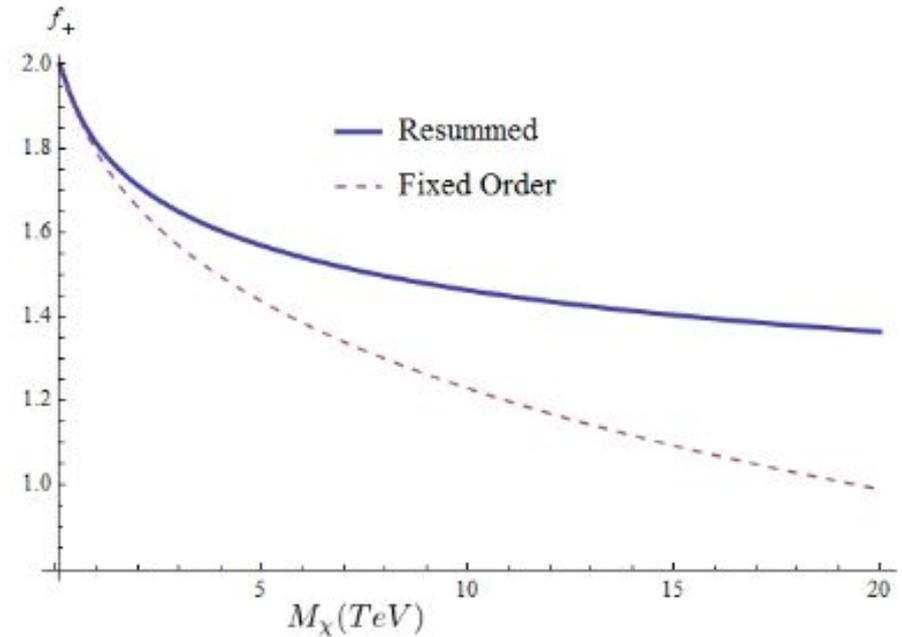
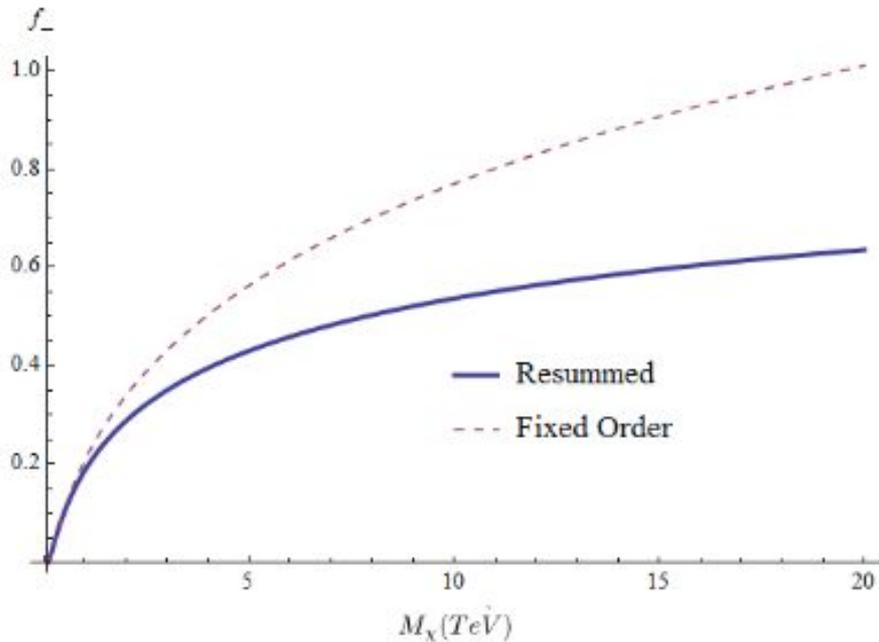
$$P_g = \frac{\alpha_W}{\pi} \left(\frac{\beta_0}{2} + 2 \int_{z_{cut}}^1 dz P_{gg}^*(z) \right),$$

$$E_1 = \exp \left[-\frac{3\alpha_W}{\pi} \log^2 \left(\frac{2M_\chi}{M_W} \right) \right],$$

$$P'_g = \frac{\alpha_W}{\pi} \left(\frac{\beta_0}{2} - \int_{z_{cut}}^1 dz P_{gg}^*(z) + 3 \right)$$

$$L = \log \left(\frac{2M_\chi}{M_W} \right)$$

$$P_{gg}^*(z) = 2 \left[z(1-z) + \frac{z}{(1-z)^+} + \frac{1-z}{z} \right]$$

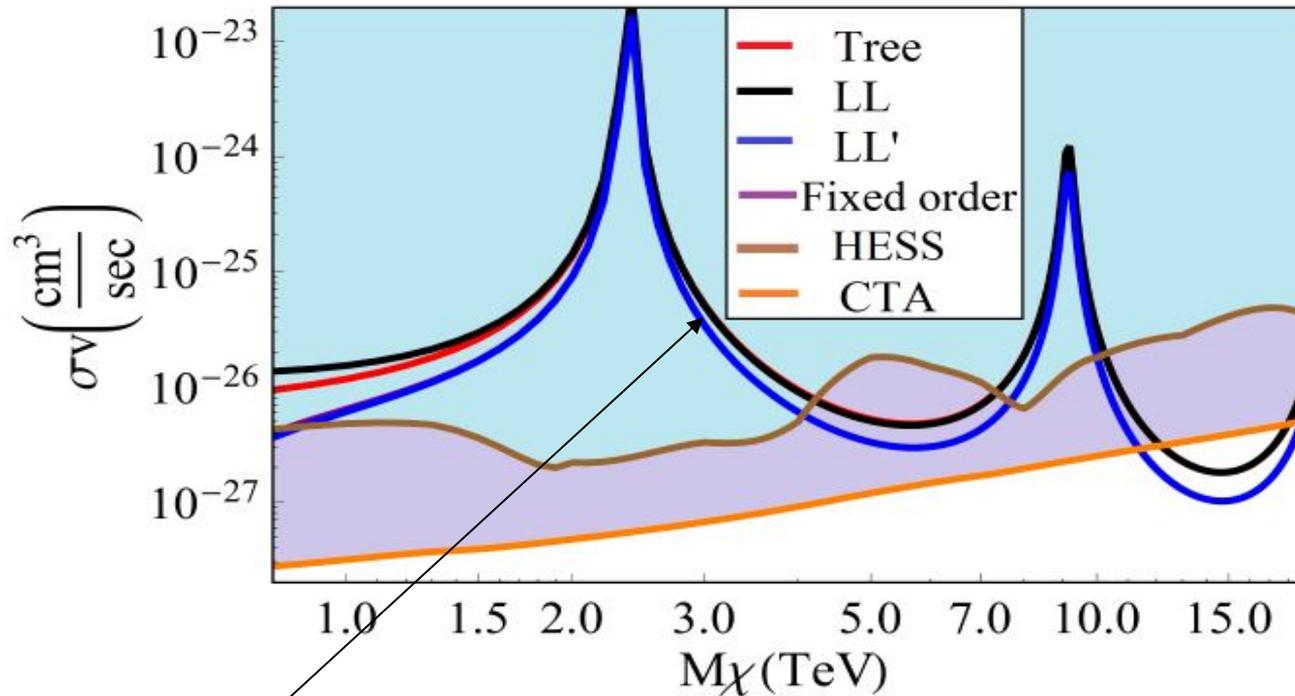


- Sudakov factors as a function of WIMP mass
- $\sim 5\%$ effect for 3 TeV thermal WINO from the dominant ($\chi^+\chi^-$) channel

Effect of resummation is small due to semi-inclusive nature of cross section

The Wino-ing

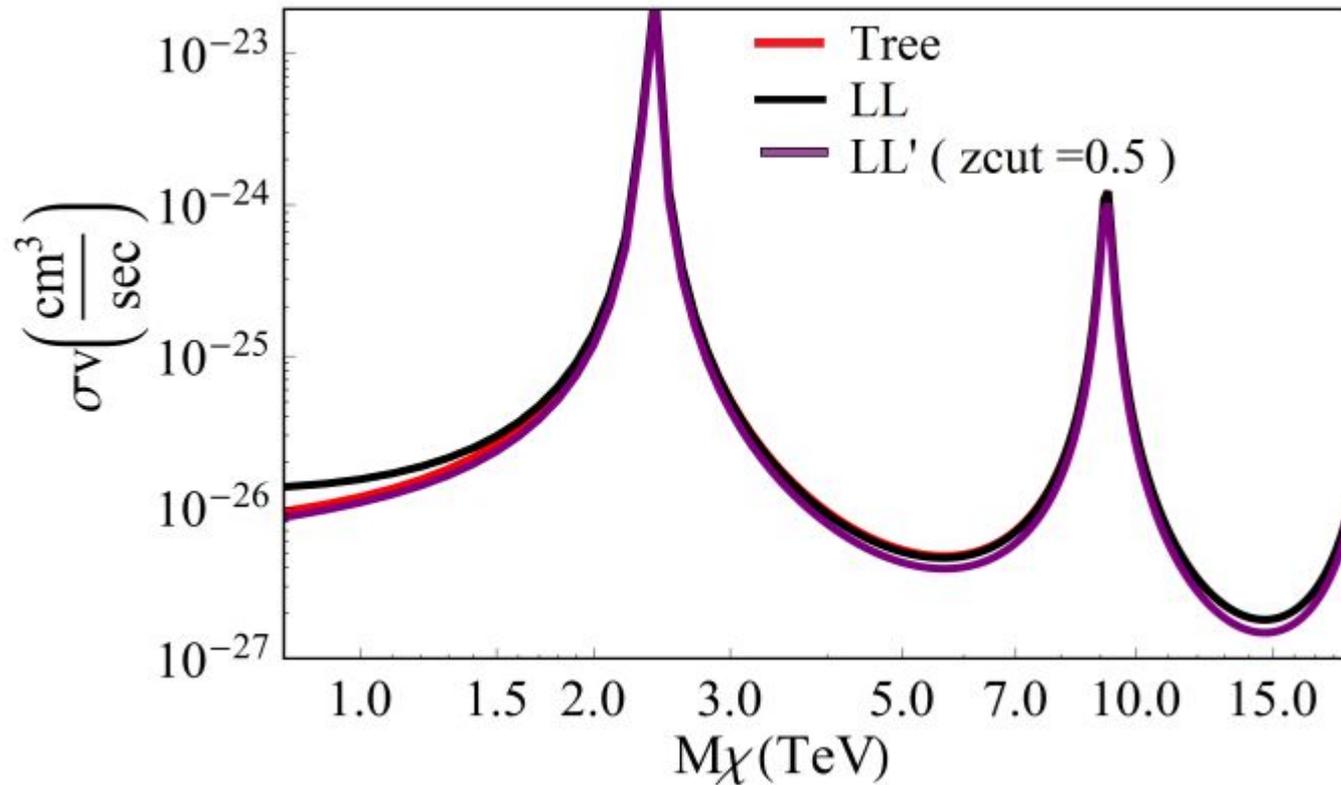
Total Rate : Sommerfeld + Sudakov



Thermal
Wino in a
lot of
trouble !

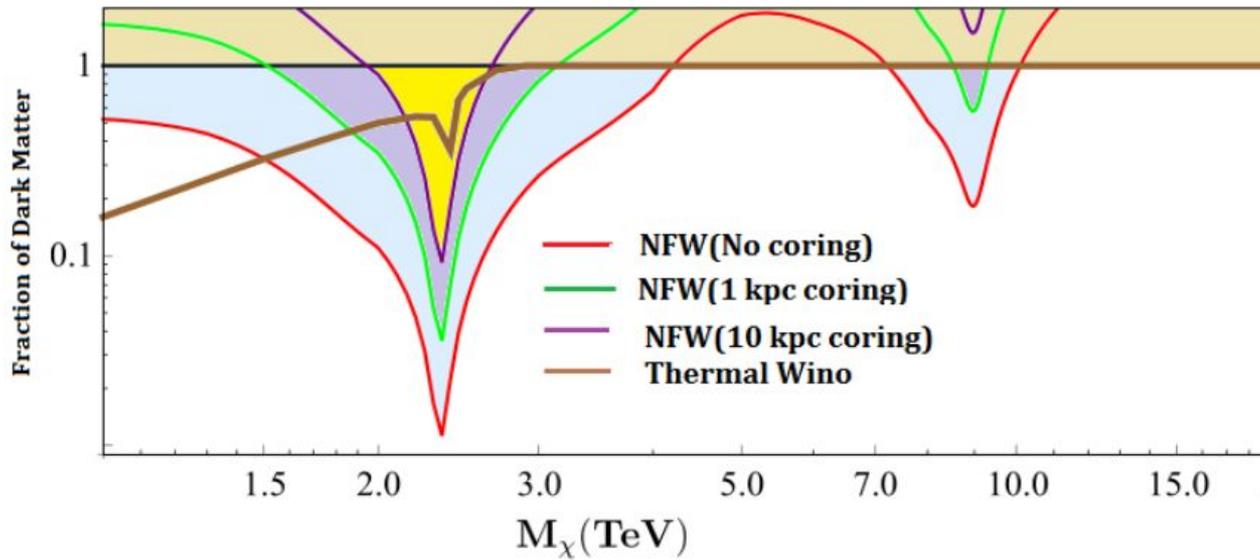
Exclusion plot using HESS with NFW profile

End point effects

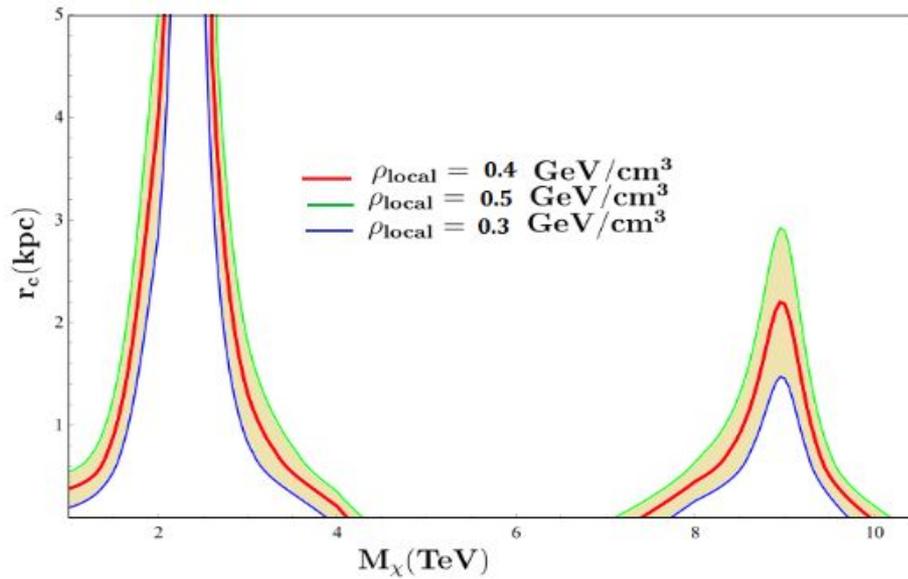


$$\log(1 - z_{cut})^2 = \log(2M_\chi/M_W)$$

$$M_\chi \approx 1.4 \text{ TeV.}$$



Viability of the Wino fraction of DM for different galactic profiles



Coring needed for the Wino to avoid exclusion

Higgsino Dark matter

Higgsino basis

$$O_1 = g^2 g'^2 \left[(\bar{\chi} \gamma^5 \tau^a \chi)(\bar{\chi} \gamma^5 \tau^a \chi) + \frac{\tan^2 \theta_W}{4} (\bar{\chi} \gamma^5 \chi)(\bar{\chi} \gamma^5 \chi) \right] B B$$

Hypercharge

$$O_2 = \frac{g^4}{4} (\bar{\chi} \gamma^5 \chi)(\bar{\chi} \gamma^5 \chi) B^A B^A$$

$$O_3 = g^2 g'^2 (\bar{\chi} \gamma^5 \tau^A \chi)(\bar{\chi} \gamma^5 \tau^B \chi) B^A B^B \longrightarrow \text{SU(2) gauge bosons}$$

$$O_4 = \left(\frac{g^3 g' + g g'^3}{2} \right) [(\bar{\chi} \gamma^5 \tau^A \chi)(\bar{\chi} \gamma^5 \chi) B^A B + (\bar{\chi} \gamma^5 \chi)(\bar{\chi} \gamma^5 \tau^A \chi) B B^A]$$

$$O_5 = (\bar{\chi} \gamma^5 \tau^A \chi)(\bar{\chi} \gamma^5 \tau^A \chi) B^B B^B.$$

$$\bar{\chi} = \begin{pmatrix} -\epsilon \tilde{h}_d & \tilde{h}_u^* \end{pmatrix} \quad \chi \equiv \begin{pmatrix} \tilde{h}_u \\ \epsilon \tilde{h}_d^* \end{pmatrix}$$

Two SU(2) doublets instead of a single triplet
State charged under hypercharge

Mass Eigenstates

$$\chi_1^0 = \frac{1}{\sqrt{2}} (h_d^0 - h_u^0)$$

$$\chi_2^0 = -\frac{i}{\sqrt{2}} (h_d^0 + h_u^0),$$

LSP

Neutralino majorana fermions

$$\chi^{+\top} = (\tilde{h}_u^+ \tilde{h}_d^{-*}).$$

Charged Dirac fermion

Remarkably we have exactly the SAME operators in the collinear and soft sectors as in the case of the WINO despite the different representation.

$$O_s^c = S_{vA'A}^\top S_{n\tilde{A}\tilde{A}}^\top$$

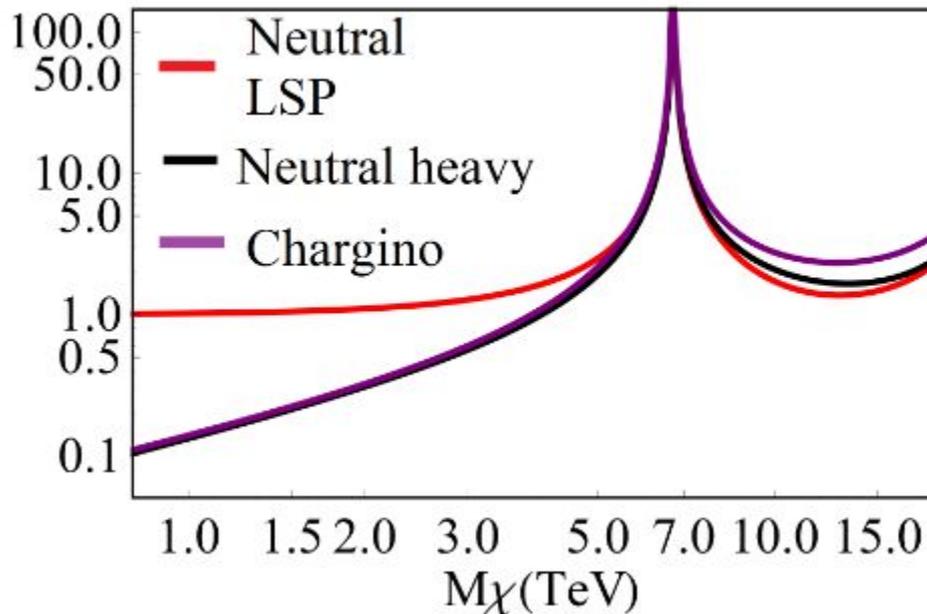
$$O_c^c = B_{\tilde{A}} B + B B_{\tilde{A}}$$

$$O_c^d = B B$$

Three new operators due to the hypercharge field

Sommerfeld factors

$$V(r) = \begin{pmatrix} 2\delta m - \frac{\alpha}{r} - \frac{\alpha_W(1-2c_W^2)^2}{4c_W^2} \frac{e^{-m_Z r}}{r} & -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{r} & -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{4r} \\ -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{4r} & 0 & -\frac{\alpha_W e^{-m_Z r}}{4c_W^2 r} \\ -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{4r} & -\frac{\alpha_W e^{-m_Z r}}{4c_W^2 r} & 2\delta m_N \end{pmatrix} \quad \psi = \begin{pmatrix} \psi_{\pm} \\ \psi_{00}^1 \\ \psi_{00}^2 \end{pmatrix}$$



$$\Delta M_+ = 350 \text{ MeV.}$$

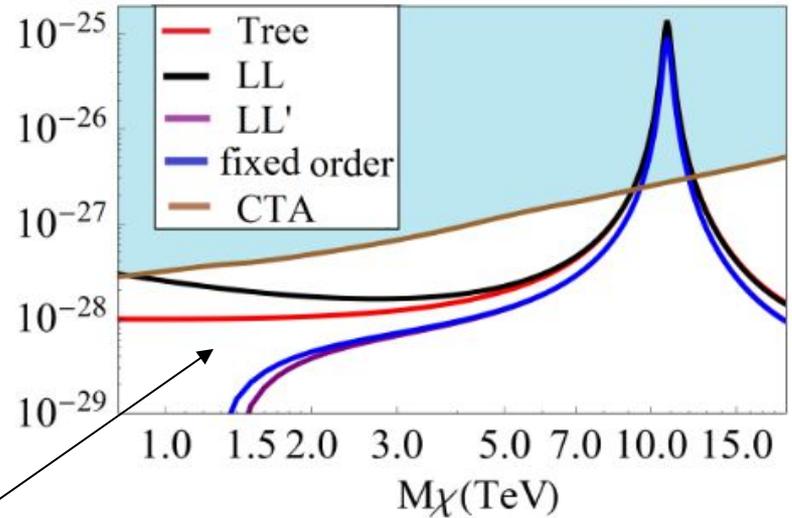
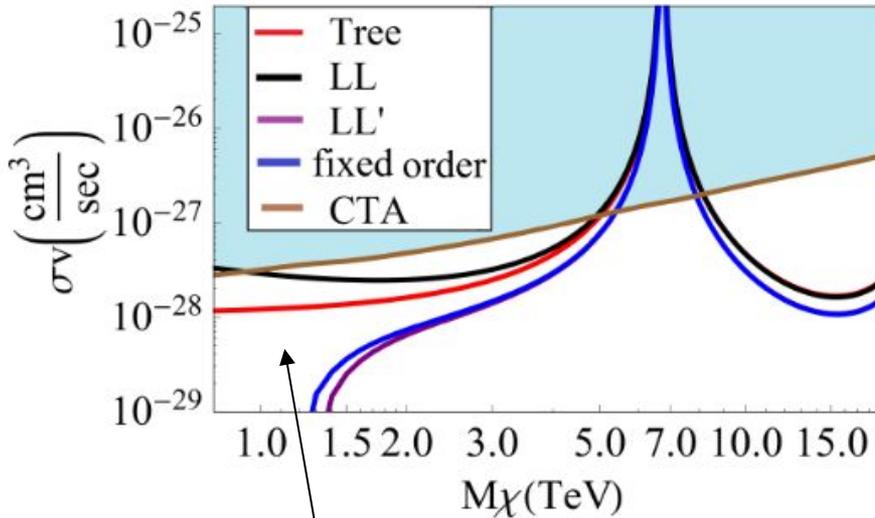
$$\Delta M = 200 \text{ keV}$$

Total Rate

$$\begin{aligned}
 \sigma v = & \frac{\pi \alpha_W \alpha'}{16 M_\chi^4} \left[\frac{1}{4} [|\psi_{00}^1(0)|^2 + |\psi_{00}^2(0)|^2 + (\psi_{00}^1 \psi_{00}^{2*} + \text{c.c.})] \times \right. \\
 & \left\{ (1 - E_2) \left\{ 1 + \left(\frac{\alpha_W}{\pi} + \frac{\alpha_W}{4\pi} \beta_0 + \frac{\alpha'}{4\pi} \beta'_0 \right) L + \Pi_{\gamma\gamma} \right\} - \frac{s_W^2}{3} (1 - E_1) (1 + P'_g L + \Pi_{\gamma\gamma}) \right. \\
 & \left. - c_W^2 \frac{\alpha_W}{\pi} \left\{ 1 - \int_{z_{cut}}^1 dz P_{gg}^*(z) \right\} L + (E_2 - s_W^2 E_1) \left(\frac{2\alpha_W}{3\pi} \right) L^2 \left(\frac{\alpha_W \beta_0}{2\pi} L + \Pi_{\gamma\gamma} \right) \right\} \\
 & + |\psi_{\pm}(0)|^2 \times \\
 & \left\{ (1 + E_2) \left\{ 1 + \left(\frac{\alpha_W}{\pi} + \frac{\alpha_W}{4\pi} \beta_0 + \frac{\alpha'}{4\pi} \beta'_0 \right) L + \Pi_{\gamma\gamma} \right\} - \frac{s_W^2}{3} (1 - E_1) (1 + P'_g L + \Pi_{\gamma\gamma}) \right. \\
 & \left. - c_W^2 \frac{\alpha_W}{\pi} \left\{ 1 - \int_{z_{cut}}^1 dz P_{gg}^*(z) \right\} L - (E_2 + s_W^2 E_1) \left(\frac{2\alpha_W}{3\pi} \right) L^2 \left(\frac{\alpha_W \beta_0}{2\pi} L + \Pi_{\gamma\gamma} \right) \right\} \\
 & + \frac{1}{2} (\psi_{00}^1 \psi_{\pm}^* + \psi_{00}^2 \psi_{\pm}^* + \text{c.c.}) \times \\
 & \left\{ \frac{s_W^2}{3} (1 - E_1) (1 + P'_g L + \Pi_{\gamma\gamma}) - s_W^2 \frac{\alpha_W}{\pi} L - (s_W^2 - c_W^2) \left\{ \frac{\alpha_W}{4\pi} \beta_0 - \frac{\alpha'}{4\pi} \beta'_0 \right\} L \right. \\
 & \left. + c_W^2 \frac{\alpha_W}{\pi} \left\{ \int_{z_{cut}}^1 dz P_{gg}^*(z) \right\} L + s_W^2 E_1 \left(\frac{2\alpha_W}{3\pi} \right) L^2 \left(\frac{\alpha_W \beta_0}{2\pi} L + \Pi_{\gamma\gamma} \right) \right\} \Bigg],
 \end{aligned}$$

Rate at LL

Higgsino bounds at LL'



$\delta M_N = 200 \text{ keV}$, $\delta M_+ = 350 \text{ MeV}$,

$\delta M_N = 2 \text{ GeV}$, $\delta M_+ = 480 \text{ MeV}$,

Unstable at low mass

$z_{cut} = 0.85$.

Summary

- A complete EFT calculation for semi-inclusive annihilation cross section to a photon of Wino/Higgsino dark matter at LL'
- Sommerfeld enhancement- a huge non-perturbative effect, puts the neutralino in trouble
- Impact of resumming Sudakov logs is minimal due to **semi-inclusive** nature of calculation
- Either we need enough coring ~ 1.5 kpc to save the thermal Wino or look for non-thermal history
- Reciprocally, the discovery of such a particle would impact astrophysical observations

End point corrections are important at low masses, needs further analysis

Evidence for dark matter

- Rotation curves of galaxies
- Gravitational lensing from galactic clusters
- Cosmological evidence : Anisotropies in CMB
- Collision of Bullet cluster with cluster 1E 0657-56

Dark Matter Candidates

Massive particle that interacts gravitationally and (possibly) weakly with SM particles (WIMP's):

- Neutrinos, Axions
- SUSY : sneutrino, gravitino, neutralino

Cold dark matter, (LSP) is stable by R parity conservation

